

PhD Course  
**Advanced Biostatistics**

Lecture 6  
**Advanced Topics.**  
**Data Analysis in Transcriptomics**

**dr. P. Nazarov**  
[petr.nazarov@lih.lu](mailto:petr.nazarov@lih.lu)

27-05-2016

- ◆ **Multiple Comparisons (L6.1)**
- ◆ **Survival analysis (L6.2)**
- ◆ **Microarray data analysis (L6.3)**
  - ◆ Principles
  - ◆ Pipeline for data analysis
  - ◆ Experiment description
  - ◆ APT import
  - ◆ QC, differential expression analysis
  - ◆ Differential expression analysis
- ◆ **RNASeq data analysis (L6.4)**
- ◆ **Enrichment analysis (L6.5)**

## Correct Results and Errors

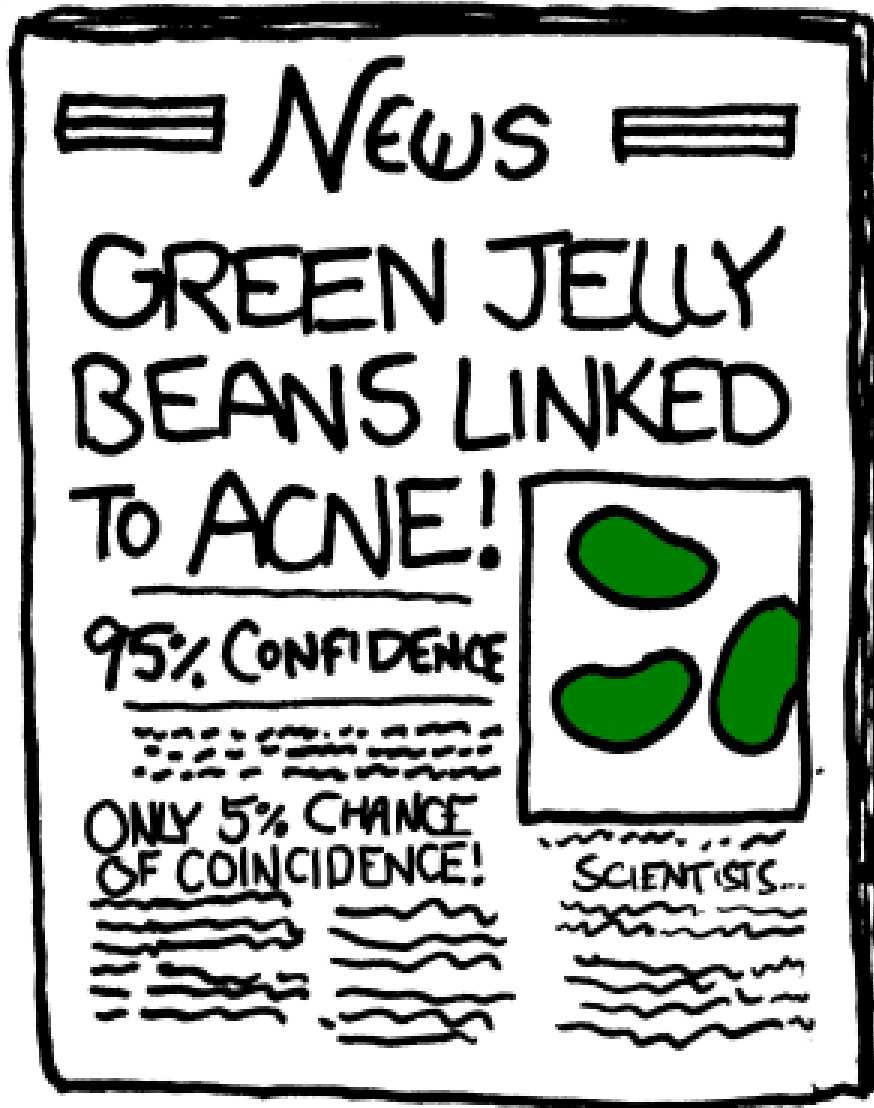
		Population Condition	
		$H_0$ True	$H_a$ True
Conclusion	Accept $H_0$	Correct Conclusion	Type II Error
	Reject $H_0$	Type I Error	Correct Conclusion

False Negative,  $\beta$  error

False Positive,  $\alpha$  error

Probability of an error in a multiple test:

$$1 - (0.95)^{\text{number of comparisons}}$$



<http://www.xkcd.com/882/>

# L6.1. Multiple Comparisons

## False Discovery Rate

### False discovery rate (FDR)

FDR control is a statistical method used in multiple hypothesis testing to correct for multiple comparisons. In a list of rejected hypotheses, FDR controls the expected proportion of incorrectly rejected null hypotheses (type I errors).

		Population Condition		Total
		H <sub>0</sub> is TRUE	H <sub>0</sub> is FALSE	
Conclusion	Accept H <sub>0</sub> (non-significant)	<i>U</i>	<i>T</i>	$m - R$
	Reject H <sub>0</sub> (significant)	<i>V</i>	<i>S</i>	$R$
	Total	$m_0$	$m - m_0$	$m$

$$FDR = E\left(\frac{V}{V + S}\right)$$

## False Discovery Rate

Assume we need to perform  $m = 100$  comparisons, and select maximum **FDR =  $\alpha = 0.05$**

### Independent tests

The **Simes procedure** ensures that its **expected value**  $\mathbf{E} \left[ \frac{V}{V + S} \right]$  is less than a given  $\alpha$  (Benjamini and Hochberg 1995). This procedure is valid when the  $m$  tests are **independent**. Let  $H_1 \dots H_m$  be the null hypotheses and  $P_1 \dots P_m$  their corresponding **p-values**. Order these values in increasing order and denote them by  $P_{(1)} \dots P_{(m)}$ . For a given  $\alpha$ , find the largest  $k$  such that  $P_{(k)} \leq \frac{k}{m} \alpha$ .

Then reject (i.e. declare positive) all  $H_{(i)}$  for  $i = 1, \dots, k$ .

Note that the mean  $\alpha$  for these  $m$  tests is  $\frac{\alpha(m+1)}{2m}$  which could be used as a rough FDR, or RFDR, " $\alpha$  adjusted for  $m$  indep. tests." The RFDR calculation shown here provides a useful approximation and is not part of the Benjamini and Hochberg method; see AFDR below.

## False Discovery Rate: Benjamini & Hochberg

Assume we need to perform  $m = 100$  comparisons, and select maximum **FDR =  $\alpha = 0.05$**

$$FDR = E\left(\frac{V}{V+S}\right)$$

Expected value for  $FDR < \alpha$  if

$$P_{(k)} \leq \frac{k}{m} \alpha$$



$$\frac{mP_{(k)}}{k} \leq \alpha$$

```
p.adjust(pv, method="fdr")
```

## Other Methods

**Bonferroni** – simple, but too stringent, not recommended

**Holm** – a more powerful and less stringent version of Bonferroni (ok)

## p-value or FDR?

Let's generate a completely random experiment (script L6.1)



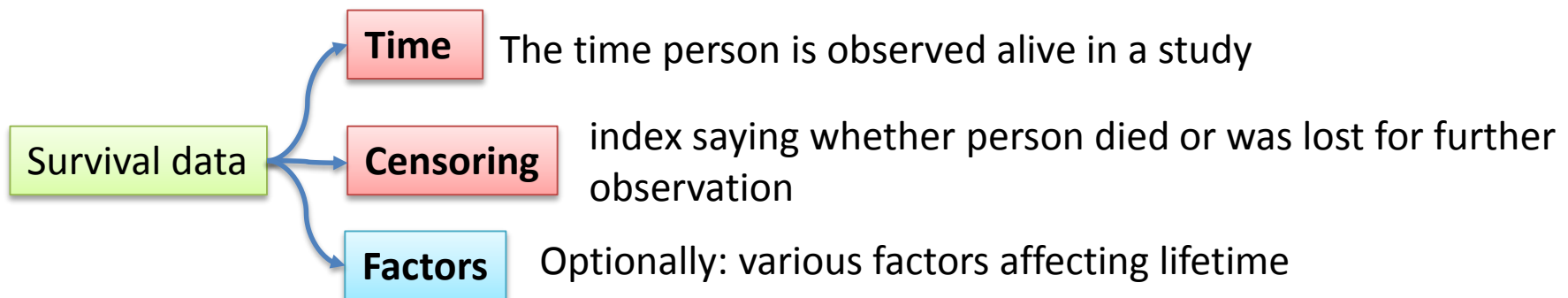
## Survival Data

### Survival analysis

is a branch of statistics which deals with analysis of time to events, such as death in biological organisms and failure in mechanical systems (i.e. **reliability theory** in engineering).

Survival analysis attempts to answer questions such as:

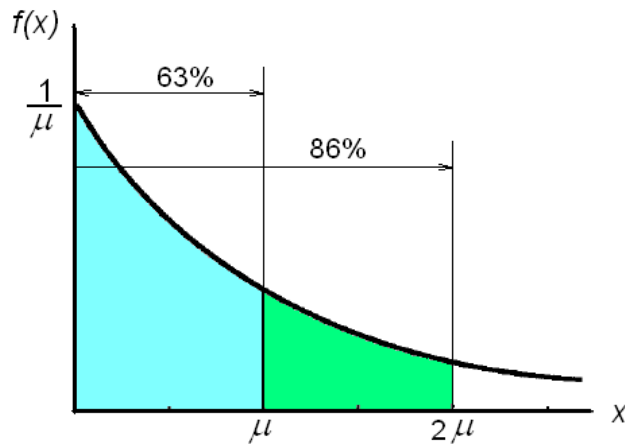
- What is the proportion of a population which will survive past a certain time?
- Of those that survive, at what rate will they die or fail?
- Can multiple causes of death or failure be taken into account?
- How do particular circumstances or characteristics increase or decrease the probability of survival?



<http://www.partek.com/webinars/survival-analysis-partek-genomics-suite-software>

## Cox's Survival Model

$$f(x) = \frac{1}{\mu} e^{-\frac{x}{\mu}} \quad \text{for } x \geq 0, \mu > 0$$



$$h(t) = h_0(t) e^{\beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n}$$

$h(t)$  – hazard function

$h_0(t)$  – basic hazard

$x_1 \dots x_n$  – covariates (age, smoking, expression of gene X)  
which are time-independent!

$\beta_1 \dots \beta_n$  – unknown parameters

$$HR = \frac{h_i(t)}{h_j(t)} = \exp\{\beta_1(x_{i1} - x_{j1}) + \dots + \beta_n(x_{in} - x_{jn})\}$$

To identify significantly involved covariate: partial likelihood is calculated

```
library(survival)
str(lung)
```

```
## create a survival object
## lung$status: 1-censored, 2-dead
sData = Surv(lung$time, event = lung$status == 2)
print(sData)
```

```
## Let's visualize it
fit = survfit(sData~1)
plot(fit)
```

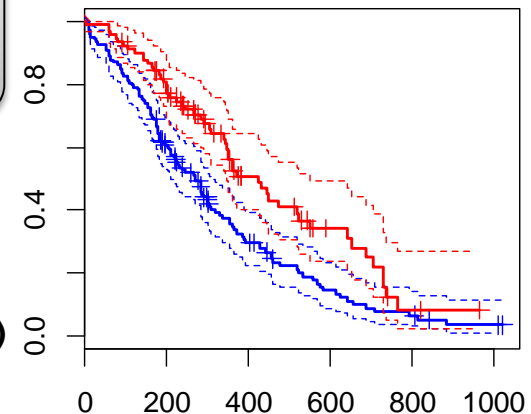
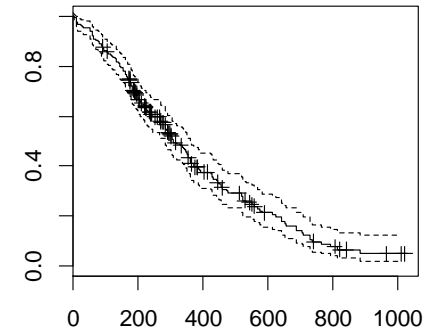
```
## Let's visualize it for male/female
fit.sex = survfit(sData ~ lung$sex)
plot(fit.sex, col=c("blue", "red"), conf.int = TRUE)
```

```
## Rank test for survival data
dif.sex = survdiff(sData ~ lung$sex)
dif.sex
```

```
## build Cox regression model
mod = coxph(sData ~ sex + age, data=lung)
summary(mod)
```

## Example: Lung

“event” should be:  
0 – for censored  
1 – for dead patients

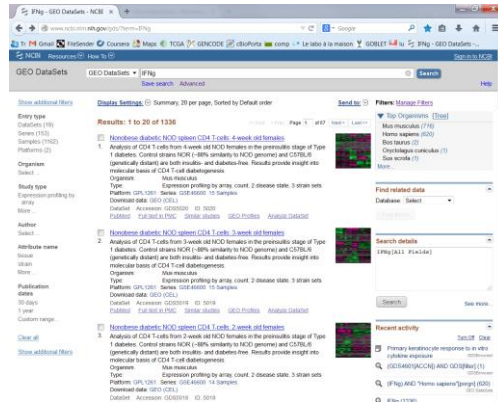


ovarian

# L6.3. Microarrays

# Public Repositories

**GEO:** <http://www.ncbi.nlm.nih.gov/gds>

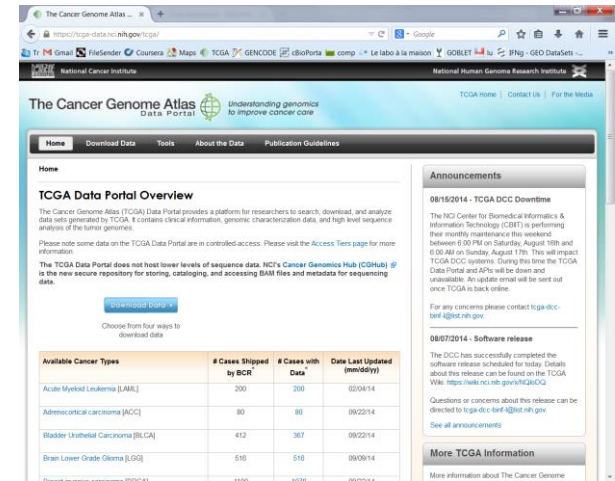


## Browse Content

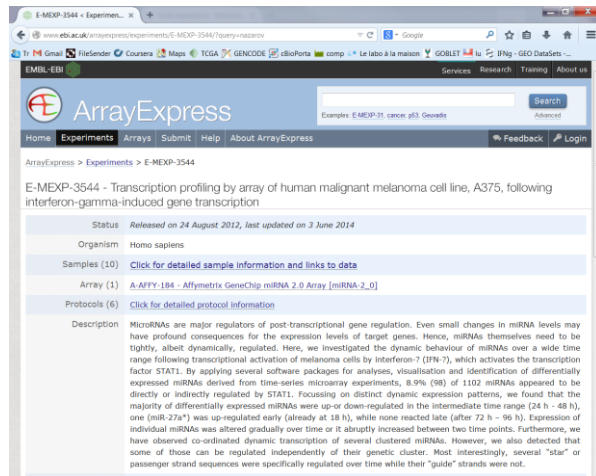
### Repository Browser

DataSets:	3847
Series:	50810
Platforms:	13387
Samples:	1237318

**TCGA:** <https://tcga-data.nci.nih.gov/tcga/>



**ArrayExpress:** <http://www.ebi.ac.uk/arrayexpress/>

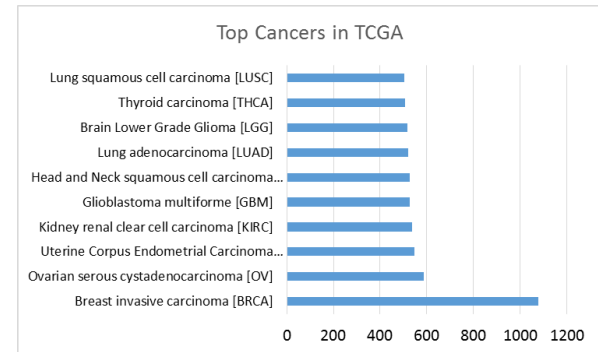


## Data Content

Updated today at 06:00

- 52801 experiments
- 1555904 assays
- 24.99 TB of archived data

Sep 2014 – more than 10k patients



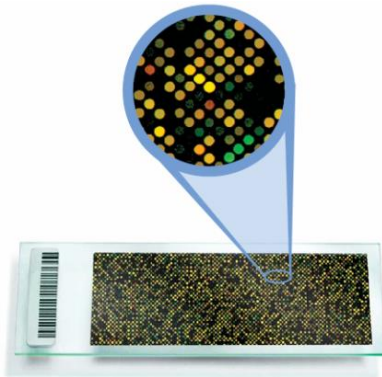
Analysis via:  
<http://www.cbioportal.org/public-portal/>

Data for our course: <http://edu.sablab.net/transcript>

## Types of Microarrays

### Two-color Arrays (2C)

- ◆ Agilent full genome
- ◆ Thematic arrays



#### Pro

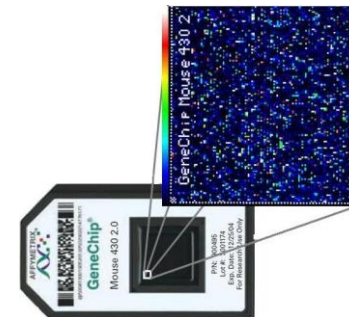
- ◆ Direct comparison
- ◆ Less sensitive to inaccuracies of spotting

#### Con

- ◆ Dye effects: need for “dye-swaps”
- ◆ Non-flexibility in analysis

### One-color Arrays (1C)

- ◆ Affymetrix GeneChip
- ◆ Affymetrix Exon
- ◆ Affymetrix mRNA



#### Pro

- ◆ Flexible analysis
- ◆ High level of standardization

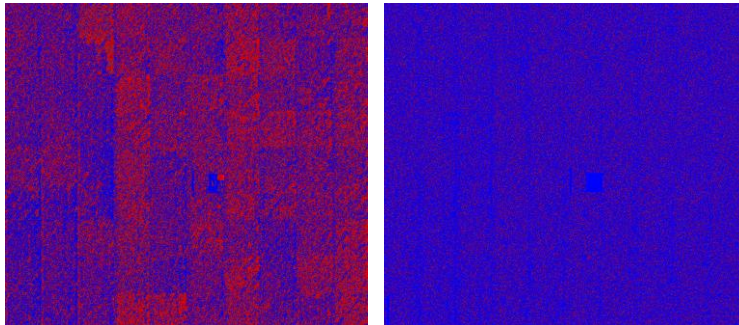
#### Con

- ◆ Price

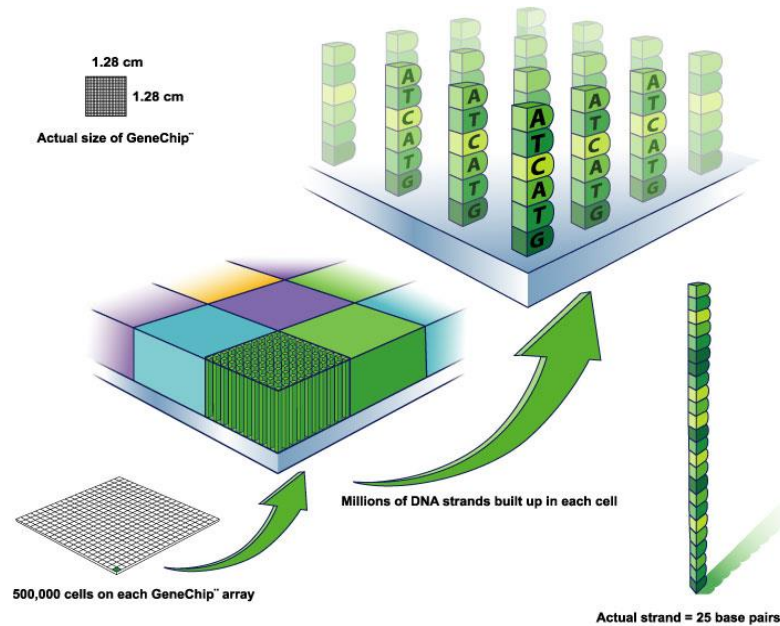
## One-color Arrays

Raw

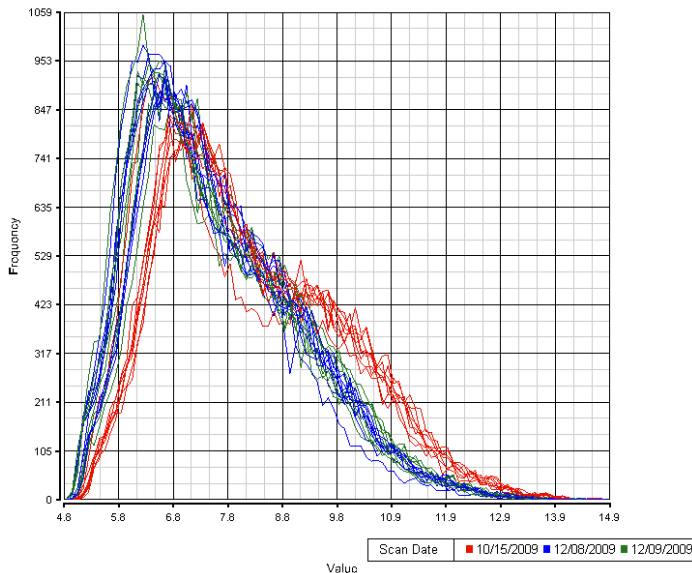
Normalized



High reproducibility and quality of spotting is required.  
Affymetrix – “photolithography”-like technique



All Rows of 1



$$\text{LogIntensity} = \log_2(I)$$

Background is “removed” during normalization step

Filtering may help removing uninformative features



## Affymetrix: Probes, Probesets and Transcript clusters

### Probes

25-mer sequences targeted on a single region of transcriptome (hopefully)

### Probesets

groups of closely located or overlapped probes (on average 4 probes)

### Exons

HuExon and HTA arrays allow measuring exon expression

### Transcript clusters

For majority of features - synonymous to "genes". However, some distinct transcripts of genes are considered as different transcript clusters.

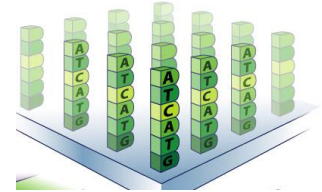
In old versions of Affy arrays (hgu95, hgu133, etc), there were:

**PM – perfect match probes**

**MM – mismatch probes** (having replacement in th 13<sup>th</sup> character)

This was done for background estimation.

**But this approach is not used now!!**

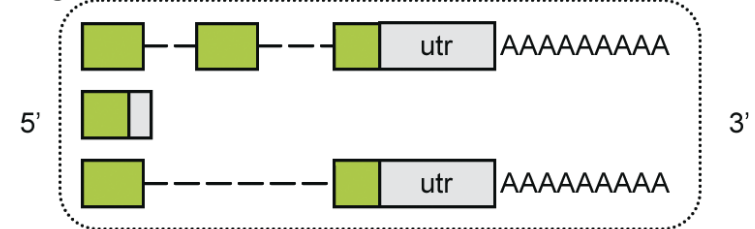


3' IVT



Probeset

gene



Exon



Okoniewski M, Comprehensive Analysis of Affymetrix Exon Arrays Using BioConductor, PLoS CompBio, 2008



## Normalization of Affymetrix Arrays by RMA

Background  
correction



Normalization  
b/w arrays



Estimate  
expression

Background and signal are strictly positive.  
Noise is additive in log scale:

$$PM_{ij} = \underbrace{S_{ijn}}_{\text{exponential}} + \underbrace{B_{ijn}}_{\text{normal}}$$

Quantile **normalization** b/w arrays: makes distribution of probes the same across all arrays

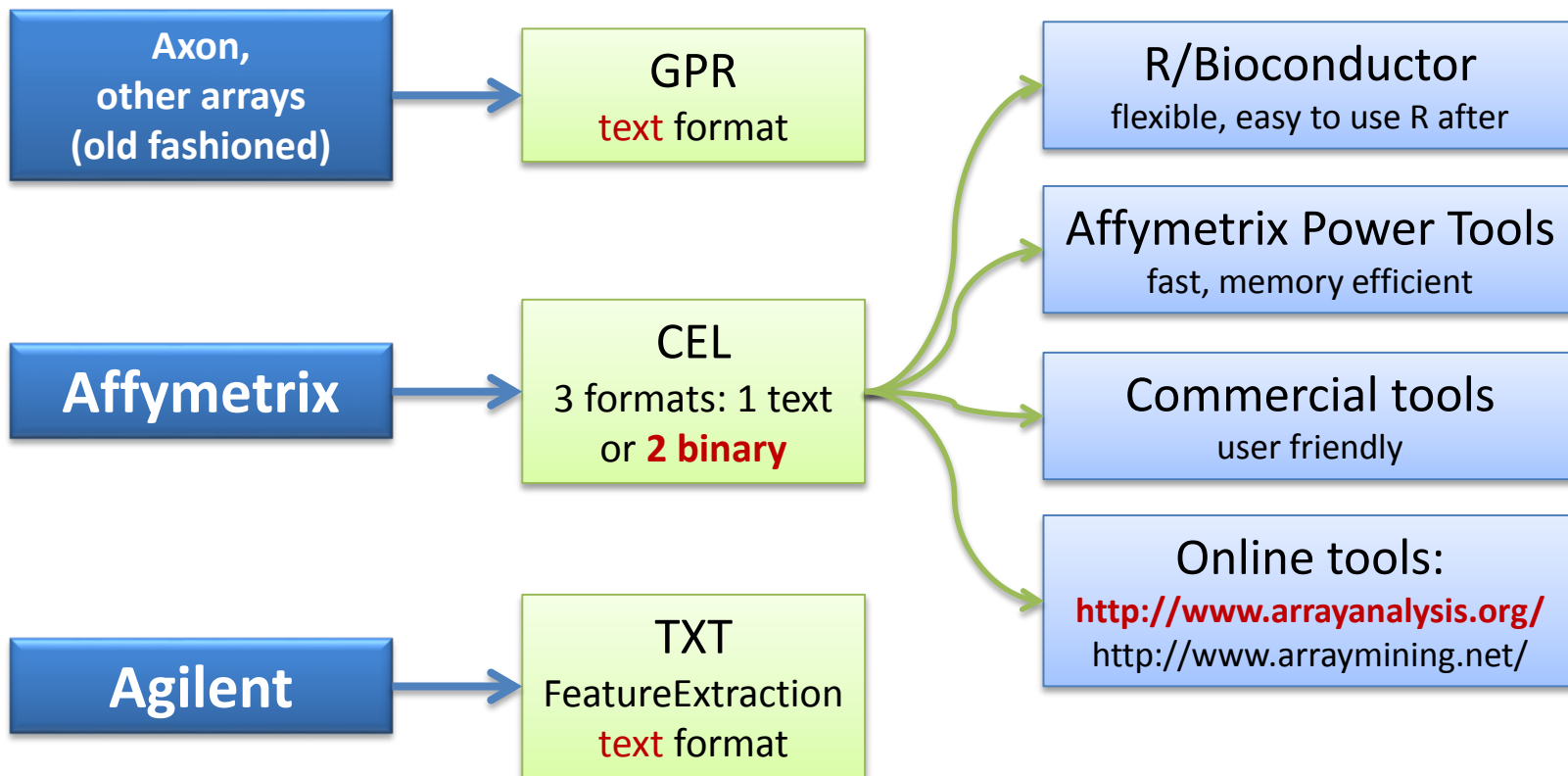
Probeset expression is estimated from a linear model:

$$Y_{ijn} = \underbrace{\mu_{in}}_{\text{observed}} + \underbrace{\alpha_{jn}}_{\text{probe affinity}} + \underbrace{\varepsilon_{ijn}}_{\text{error with 0 mean}}$$

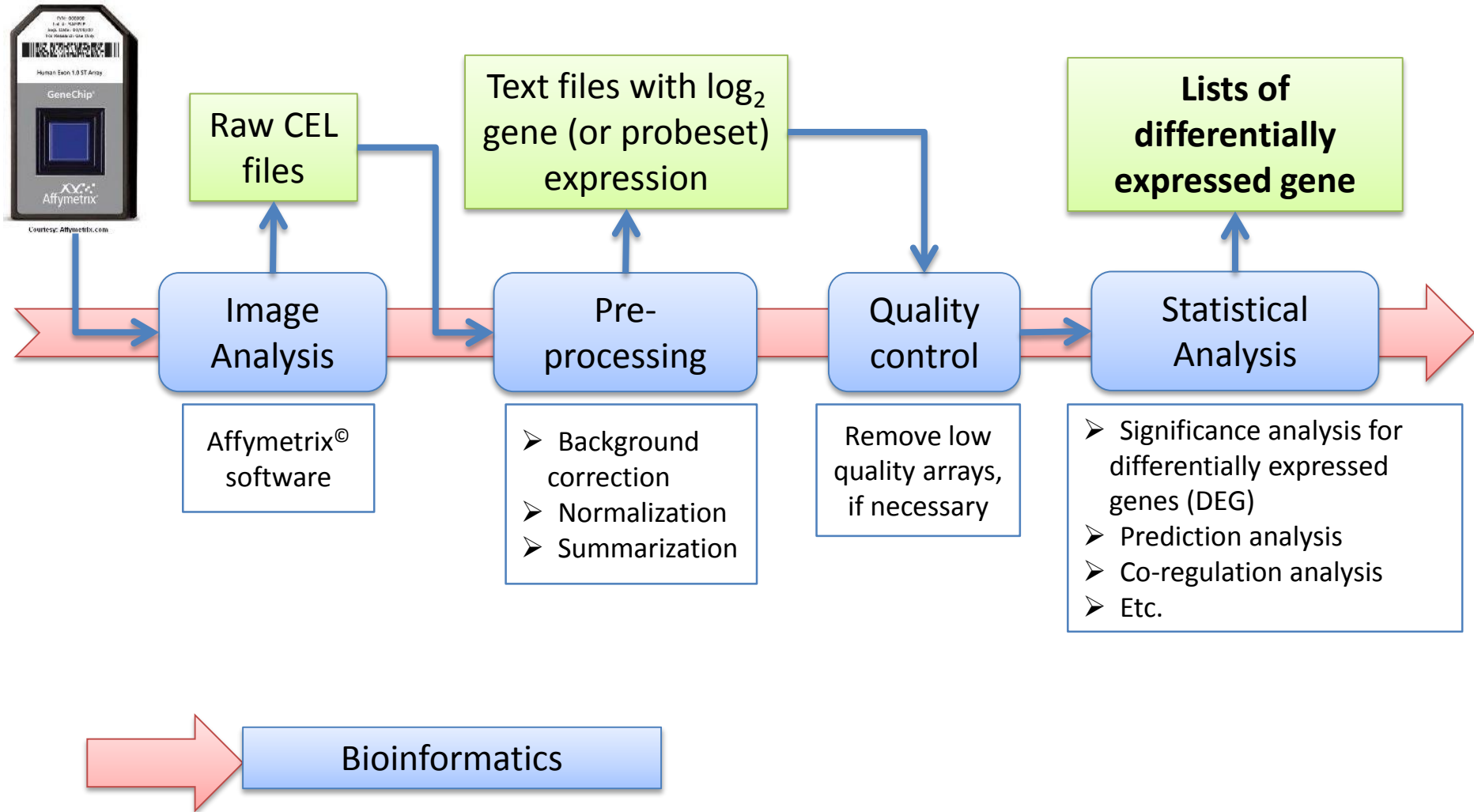
i -- array  
j -- probe  
n -- probeset

“Median polish” helps avoid outliers effect

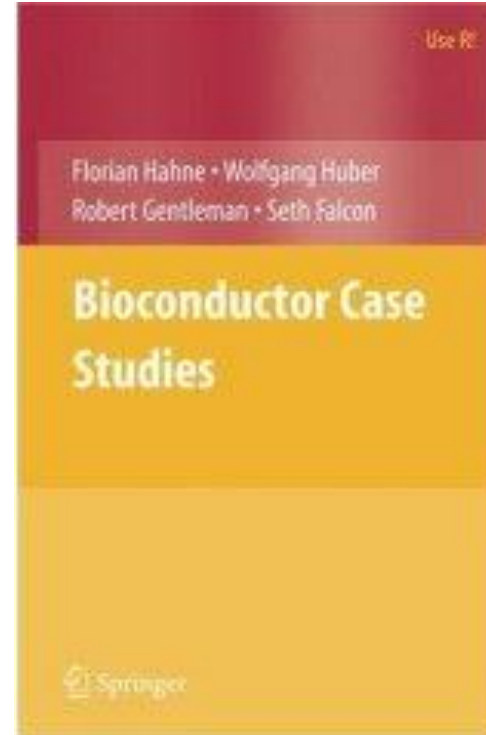
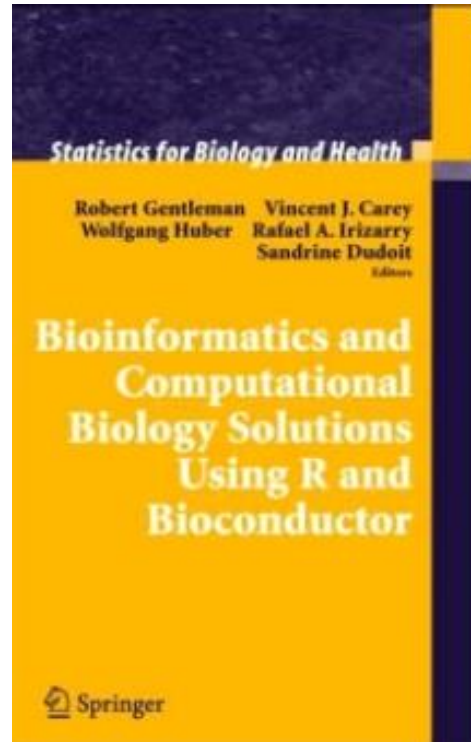
## File Formats



## Analysis Pipeline



## R / Bioconductor



## Affymetrix Power Tools

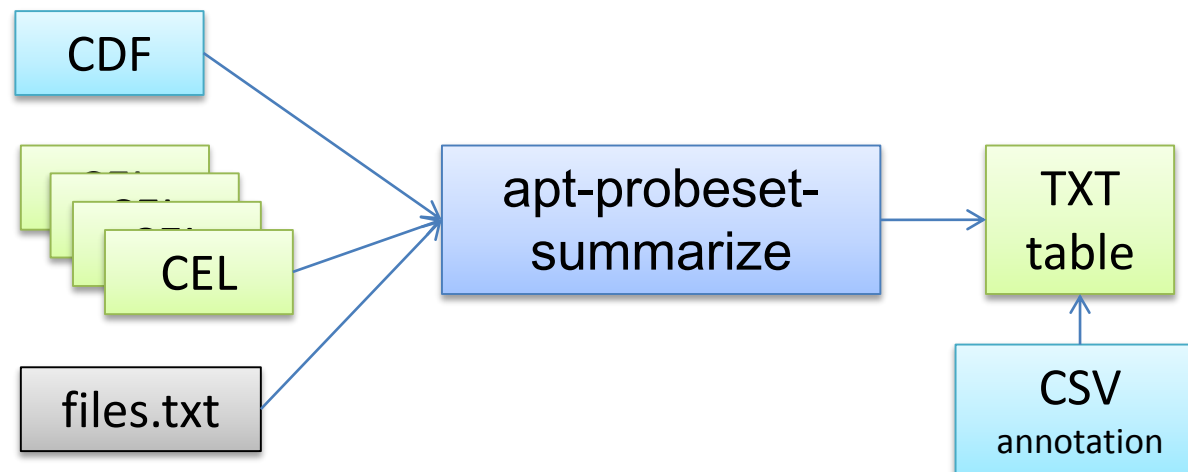
**apt-probeset-summarize** is a program for doing background subtraction, normalization and summarizing probe sets from Affymetrix expression microarrays. It implements analysis algorithms such as [RMA](#), [Plier](#), and DABG (detected above background).

The main features of **apt-probeset-summarize** not common in other implementations are: Quantile normalization using a subset (sketch) of the data which results in much smaller memory usage.

<http://www.affymetrix.com/support/developer/powertools/changelog/apt-probeset-summarize.html>

### apt-probeset-summarize

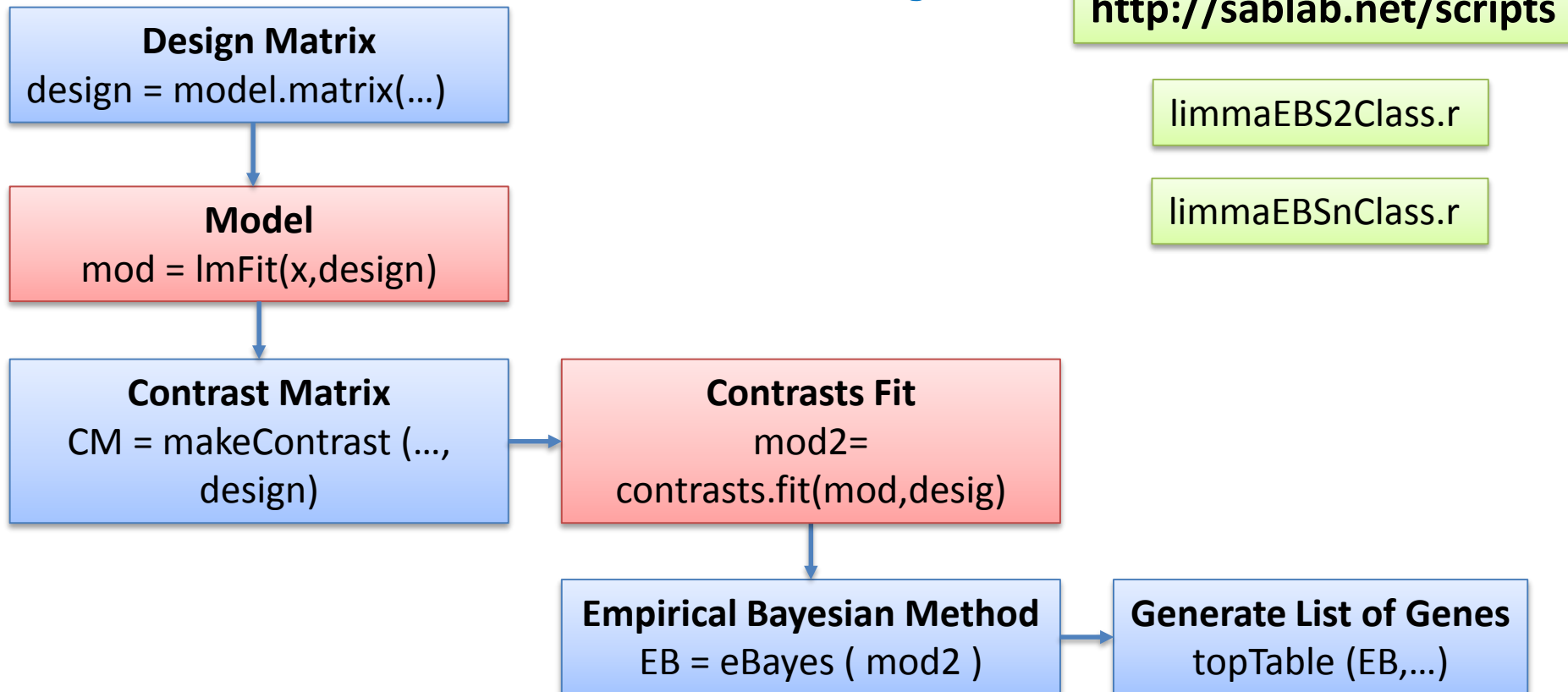
```
-a rma-sketch -d chip.cdf -o output-dir --cel-files files.txt
```



<http://edu.sablab.net/data/gz/>

## Differential Expression Analysis

### Factorial design

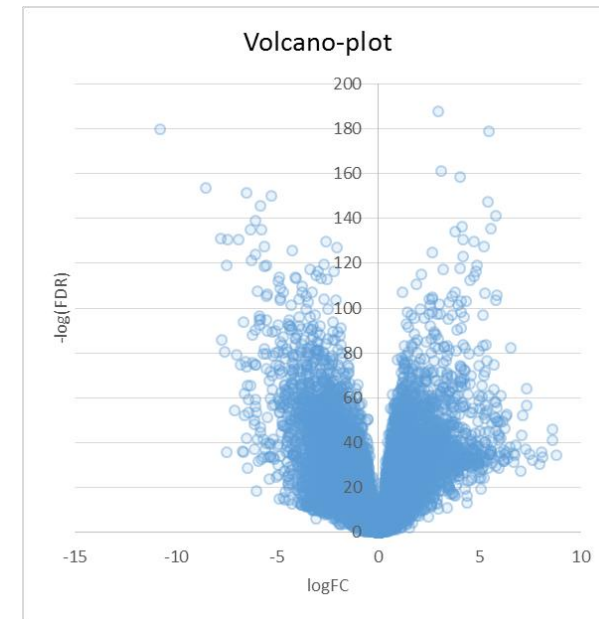


## Differential Expression Analysis

<http://edu.sablab.net/data/txt/lusc.zip>

1. Find genes significantly differentially expressed in SCC vs normal tissue
  - apply *limma*
  - Keep genes with  $FDR > 0.001$
  - keep only genes with  $|\logFC| > 2$
2. Make a “volcano plot”:
  - $\log_{10}(FDR)$  vs  $\logFC$
3. Save lists of up and down regulate genes – we shall need them

<http://sablab.net/scripts>





```
#####
# L6.2. Import and Analysis
#####
## clear memory
rm(list = ls())

##-----
## L6.2.1. Loading results after APT and QC
##-----

## load data after APT
## alternative: http://edu.sablab.net/data/gz/rma-sketch.summary.txt
Data = read.table("e:/data/kreis/+data+/miR.pub/cel/res/rma-sketch.summary.txt",
                  header=T, sep="\t", as.is=T)

## load sample description
## alternative: http://edu.sablab.net/data/gz/Affymetrix_miRNA2.txt
Meta= read.table("e:/data/kreis/+data+/miR.pub/cel/files.txt",
                 header=T, sep="\t", as.is=T)

str(Data)
Meta

## keep only human miRNA
Data = Data[grep("hsa-",Data$probeset_id),]

# if order of Data columns and Meta rows are the same - simply change columns
if (sum(names(Data[, -1])!= Meta[,1]) == 0) names(Data)[-1] = Meta[,2]

source("http://sablab.net/scripts/plotDataPDF.r")
x11()
plotDataPDF(Data,add.legend=T,col=rainbow(ncol(Data)))
x11()
boxplot(Data[, -1],outline=F,col=rainbow(ncol(Data)),las=2)

#####
##-----
## L6.2.2 Analysis
##-----

## let's filter out miR with low expression
## and put the rest into matrix Y
thr = 3
idx.keep = logical(nrow(Data))|T
idx.keep[apply(Data[, -1],1,max)<=thr]=F
sum(idx.keep)

## Y contains now the data
Y = as.matrix(Data[idx.keep, -1])
colnames(Y) = names(Data)[-1]
rownames(Y) = sub("_st","",Data[idx.keep,1])
str(Y)

## plot heatmap of scaled data
heatmap(t(scale(t(Y))))

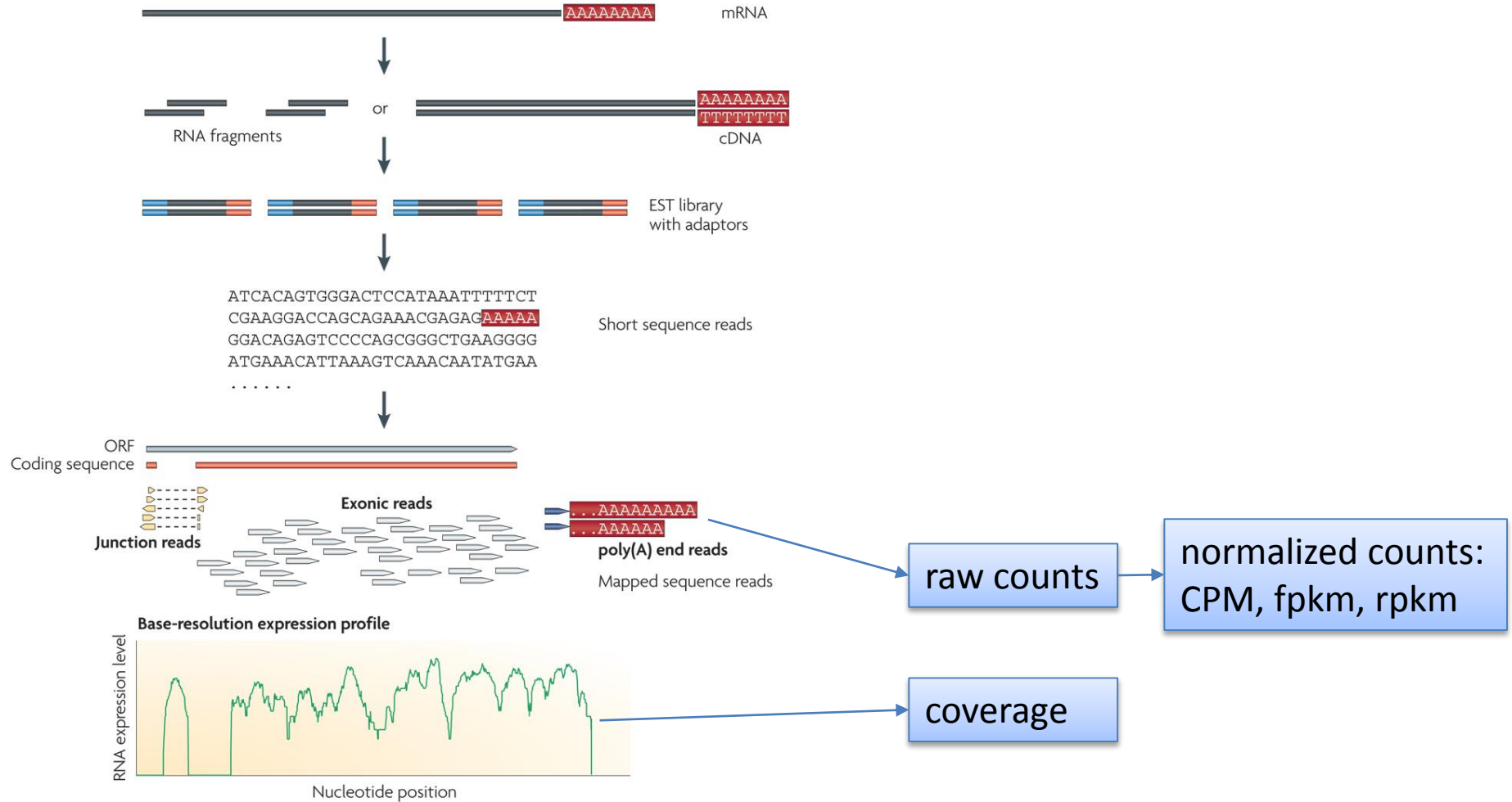
## plot PCA
PC = prcomp(t(Y))
## plot 3D
library(rgl)
plot3d(PC$x[,1],PC$x[,2],PC$x[,3],
       size = 2,
       col = rainbow(ncol(Data)),
       type = "s",
       xlab = "PC1",
       ylab = "PC2",
       zlab = "PC3")
text3d(PC$x[,1]+0.5,PC$x[,2]+0.5,PC$x[,3]+0.5,colnames(Y))

## DEA
source("http://sablab.net/scripts/limmaEBS2Class.r")

idx=c(grep("T000",colnames(Y)),
      grep("T48",colnames(Y)))
res=limmaEBS2Class(Y[,idx],rownames(Y),classes=c("T00","T00","T48","T48"),
                  plotTop=20)
```

# RNASeq

## Next Generation Sequencing: RNA-Seq



Wang Z et al. RNA-Seq: a revolutionary tool for transcriptomics. **Nat Rev Genet.** 2009



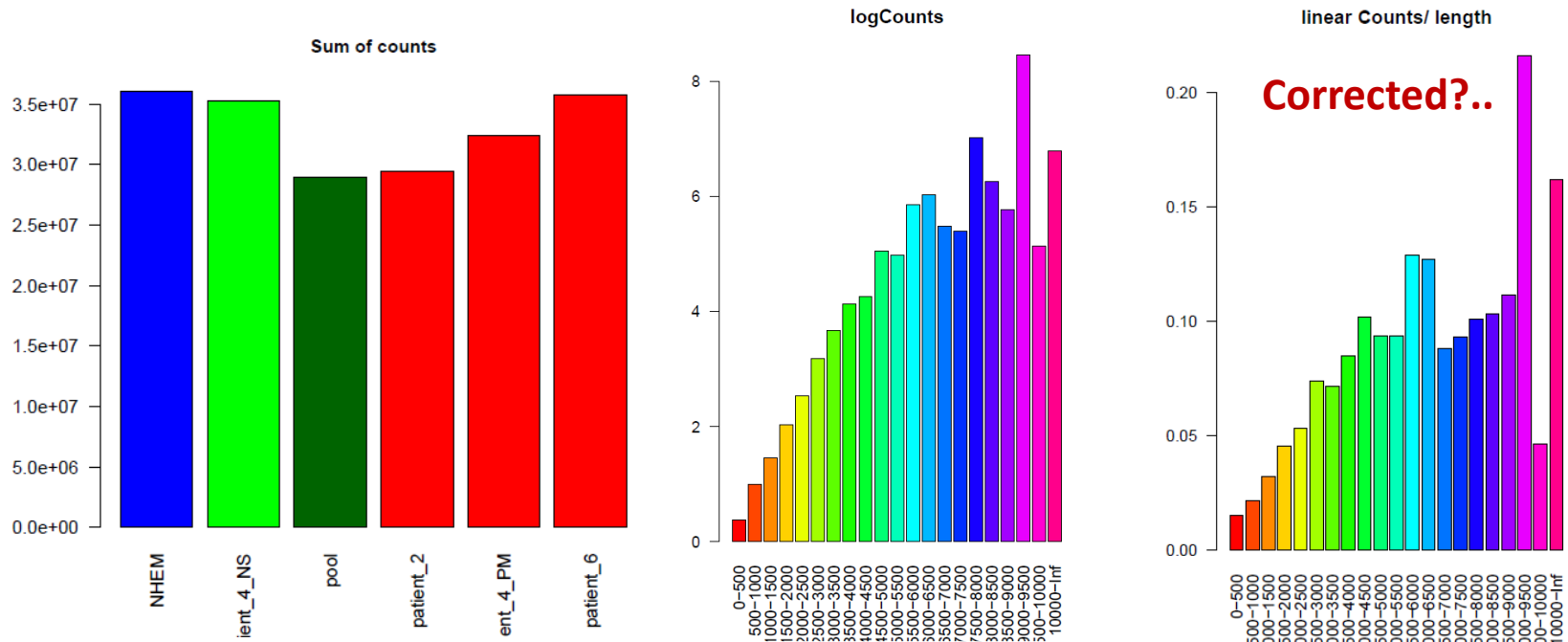
## Normalization

### Problems:

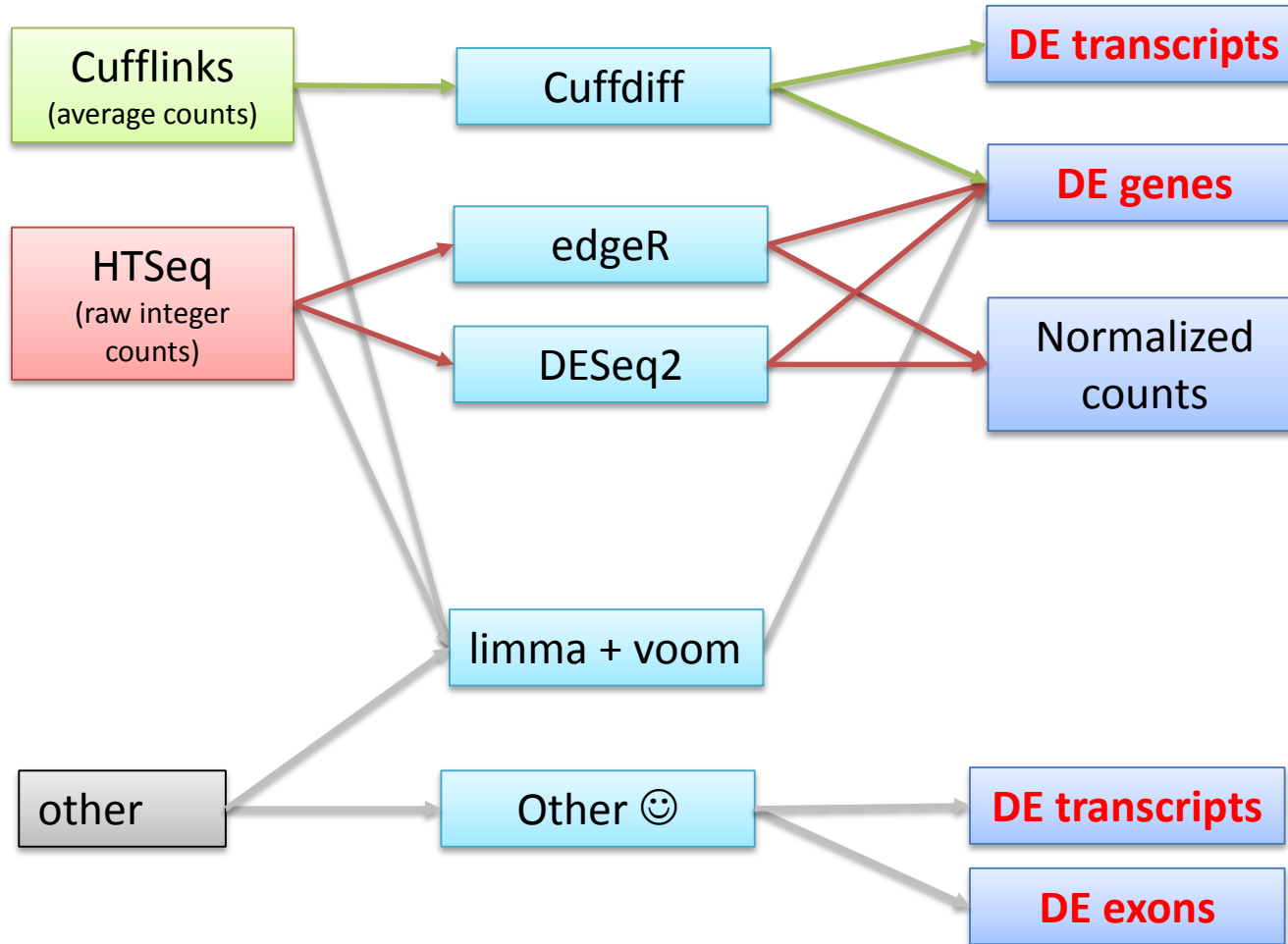
- ◆ Libraries has different size (different number of reads from samples)
- ◆ Long transcripts produce more reads

### Solutions (?) :

- ◆ Accounting for library size during analysis (standard) or direct correction for it
- ◆ Correction for transcript size (but which transcript is expressed?)



## Differential Expression Analysis



## Differential Expression Analysis (edgeR)

<https://sablabs.net/scripts>

LibDEA.r

## Differential Expression Analysis (DESeq2)

<https://sablabs.net/scripts>

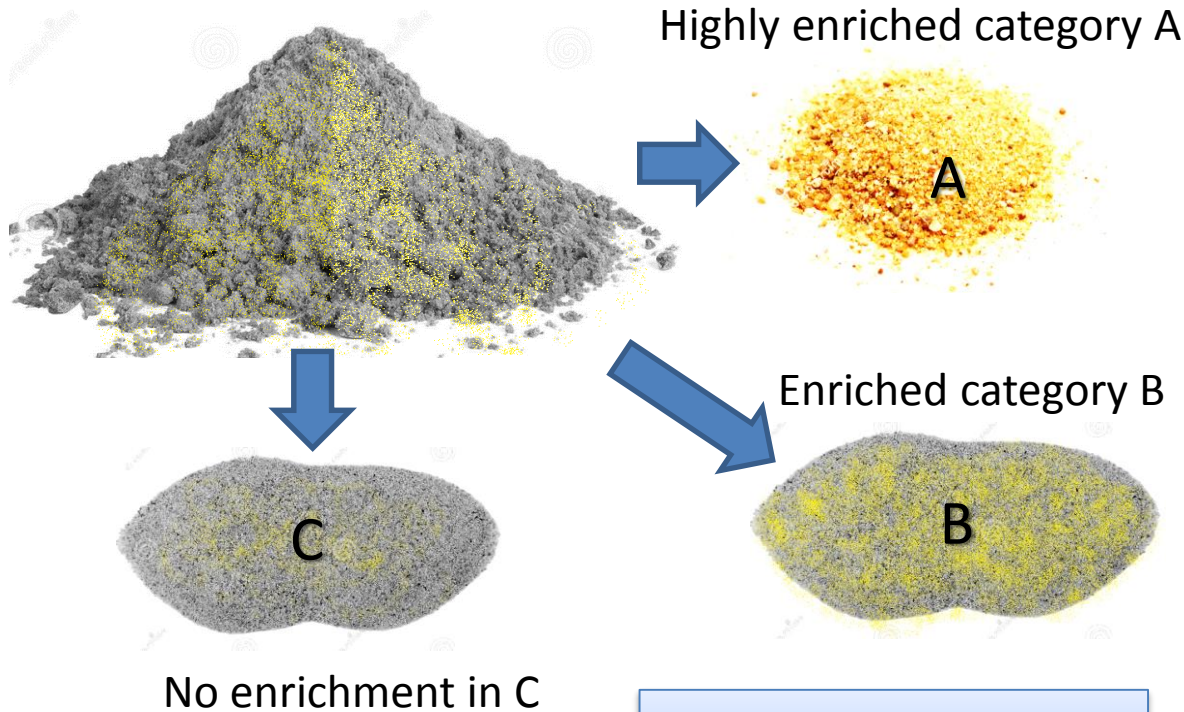
LibDEA.r

# Enrichment Analysis



## 1. Category Enrichment Analysis

Are interesting genes overrepresented in a subset corresponding to some biological process?



Someone grabs “randomly” 20 balls from a box with 100x ● and 100x ●

How surprised will you be if he grabbed

●●●●●●●●●●●●●●●●●●●● (17 red , 3 green)

Method of the analysis:  
**Fisher’s exact test**

sand belongs to: <http://www.dreamstime.com/photos-images/pile-sand.html> ;))

## 1. Category Enrichment Analysis

**Fisher's exact test:** based on hypergeometrical distributions

Hypergeometrical: distribution of objects taken from a "box", without putting them back

$$P = 1 - \sum_{i=0}^{k-1} \frac{\binom{M}{i} \binom{N-M}{n-i}}{\binom{N}{n}}$$

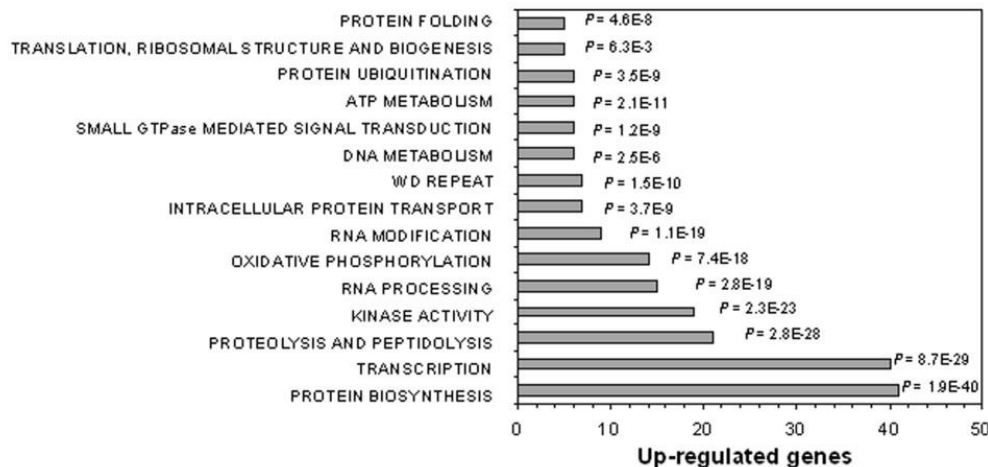
N: total number of genes

M: total number of genes annotated with this term

n: number of genes in the list

k: number of genes in the list annotated with this term

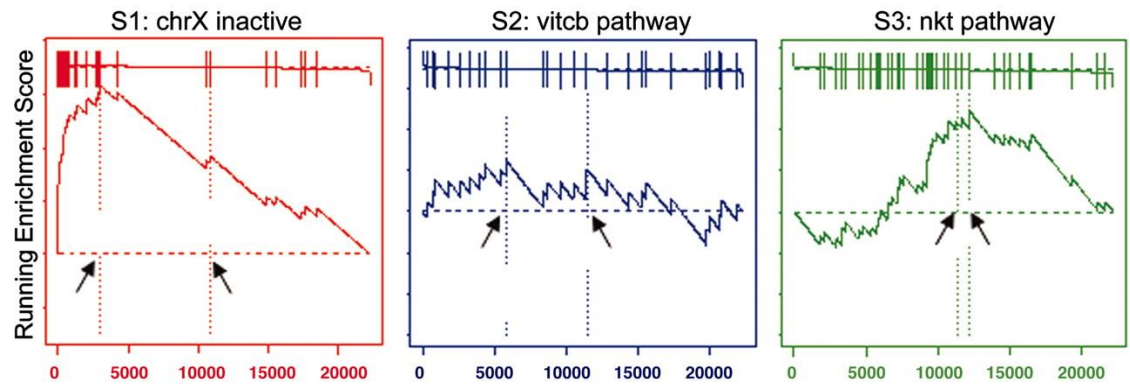
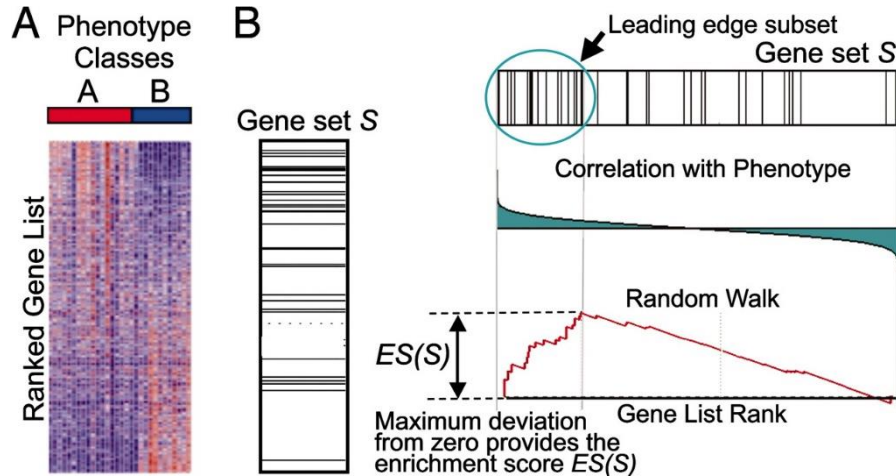
$$C_k^n = C_n^k = \binom{n}{k} = \frac{n!}{k!(n-k)!}$$



Okamoto et al. Cancer Cell International 2007 7:11 doi:10.1186/1475-2867-7-11

## 2. Gene Set Enrichment Analysis (GSEA)

Is direction of genes in a category random?



A. Subramanian et al. PNAS 2005,102,43

## Example: GO enrichment

<http://edu.sablab.net/transcript>

### Strategy 1:

Take all DEG and use them in enrichment.

- Safe
- No additional assumptions
- Cannot distinguish  $\uparrow$  and  $\downarrow$  functions

### Strategy 2:

Separate DEG to down- and up- regulated genes. Then perform independent enrichment by these 2 groups

- Can be biased (gene can be  $\uparrow\downarrow$ )
- Assume  $\uparrow$ gene  $\Rightarrow$   $\uparrow$ function
- Can distinguish  $\uparrow$  and  $\downarrow$  functions

### Enrichr

<http://amp.pharm.mssm.edu/Enrichr/enrich>

### BioCompendium

<http://biocompendium.embl.de/>

## LUSC Example

<http://edu.sablab.net/data/txt/lusc.zip>

<http://amp.pharm.mssm.edu/Enrichr/>

0. Prepare lists of DE genes...

1. Put up-regulated into **enrich**

3. Check: Down CMAP, Disease Signatures from GEO up,

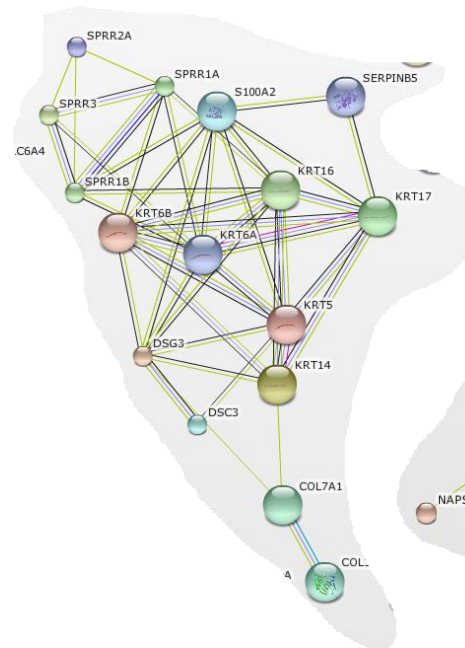
4. Try **biocompendium**

5. Put top 100 genes into String to see PP-interactions

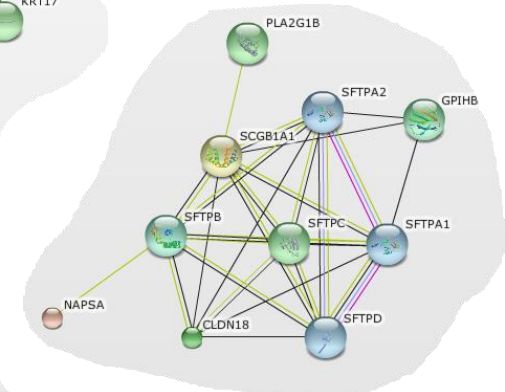
<http://biocompendium.embl.de/>

<http://string-db.org>

**Up regulated**



**Down regulated**



## In R

```
#####
## enrichGOens - warpup for topGO package: enrichment analysis of GO-terms
## based on Ensembl IDs
#####
## genes - vector with list of ENSEMBL IDs (character)
## fdr - vector of FDR for each gene (numeric)
## fc - vector of logFC for each gene (numeric)
## thr.fdr - significance threshold for FDR (numeric)
## thr.fc - significance threshold for absolute logFC (numeric)
## db - name of GO database: "BP", "MF", "CC" (character)
## genome - R-package for genome annotation used. For human - 'org.Hs.eg.db' (character)
## do.sort - if TRUE - resulted functions sorted by p-value (logical)
## randomFraction - for testing only, the fraction of the genes to be randomized (numeric)
#####
## (c)GNU GPL P.Nazarov 2014. petr.nazarov[at]crp-sante.lu
#####
```

```
enrichGOens =
function (genes, fdr, fc, thr.fdr=0.05, thr.fc=0, db="BP", genome="org.Hs.eg.db", do.sort=TRUE,
        randomFraction=0) {
  ## load libraries
  if (!require(genome, character.only=TRUE)){
    cat("MESSAGE enrichGO: '", genome, "' package is not found. Installing...\n", sep="")
    source("http://bioconductor.org/biocLite.R")
    biocLite(genome)
    library(genome, character.only=TRUE)
  }
  if (!require("topGO")){
    cat("MESSAGE enrichGO: ' topGO ' package is not found. Installing...\n")
    source("http://bioconductor.org/biocLite.R")
    biocLite("topGO")
    library("topGO")
  }
  if (!exists("sortDataFrame")) source("http://sablabs.net/scripts/sortDataFrame.r")
  ## prepare gene categories and score
  myGO2genes <- annFUN.org(db, mapping = "org.Hs.eg.db", ID = "ensembl")
  score = (-log10(fdr)*abs(fc))
  names(score)=genes
  score[fdr>thr.fdr | abs(fc)<=thr.fc]=0

  ## add randomness if required, to test stability
  if (randomFraction>0){
    ## define remove probability: low score have more chances
    prob1 = 1/(1+score)
    prob1[is.na(prob1)]=0
    prob1[score == 0] = 0
    ## define add probability: high score has more chances
    prob2 = -log10(fdr)*abs(fc)
    prob2[is.na(prob2)]=0
    prob2[score > 0] = 0
    ## add and remove
    n=round(sum(score>0)*randomFraction)
    score[sample(1:length(genes), n, prob=prob2)]=1+rexp(n, 1/mean(score[score>0]))
    score[sample(1:length(genes), n, prob=prob1)]=0
  }
  ## create topGOdata object
  SelectScore = function(sc){return(sc>0)} ## simple function for significance
  GOdata = new("topGOdata", ##constructor
    ontology = db,
    allGenes = score,
    geneSelectionFun = SelectScore,
    annot = annFUN.GO2genes,
    GO2genes = myGO2genes)

  ## run testing
  resFisher = runTest(GOdata, algorithm = "classic", statistic = "fisher")
  ## transform results into a table
  enrichRes = GenTable(GOdata, classicFisher = resFisher,
    ranksOf = "classicFisher", topNodes = length(resFisher$score))
  enrichRes$classicFisher[grepl("<", enrichRes$classicFisher)] = "1e-31"
  enrichRes$classicFisher = as.double(enrichRes$classicFisher)
  enrichRes$FDR = p.adjust(enrichRes$classicFisher, "fdr")
  enrichRes$Score = -log10(enrichRes$FDR)
  ## by default sorted by p-value. If needed - sort by ID
  if (!do.sort) enrichRes = sortDataFrame(enrichRes, "GO.ID") ## remove sorting
  return(enrichRes)
}
```

<https://sablabs.net/scripts>

enrichGOens.r

# Thank you for your attention !

