

PhD Course
Advanced Biostatistics

Lecture 6
Advanced Topics.
Data Analysis in Transcriptomics

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- ◆ **Multiple Comparisons (L6.1)**
- ◆ **Survival analysis (L6.2)**
- ◆ **Microarray data analysis (L6.3)**
 - ◆ Principles
 - ◆ Pipeline for data analysis
 - ◆ Experiment description
 - ◆ APT import
 - ◆ QC, differential expression analysis
 - ◆ Differential expression analysis
- ◆ **RNASeq data analysis (L6.4)**
- ◆ **Enrichment analysis (L6.5)**

L6.1. Multiple Comparisons

Correct Results and Errors

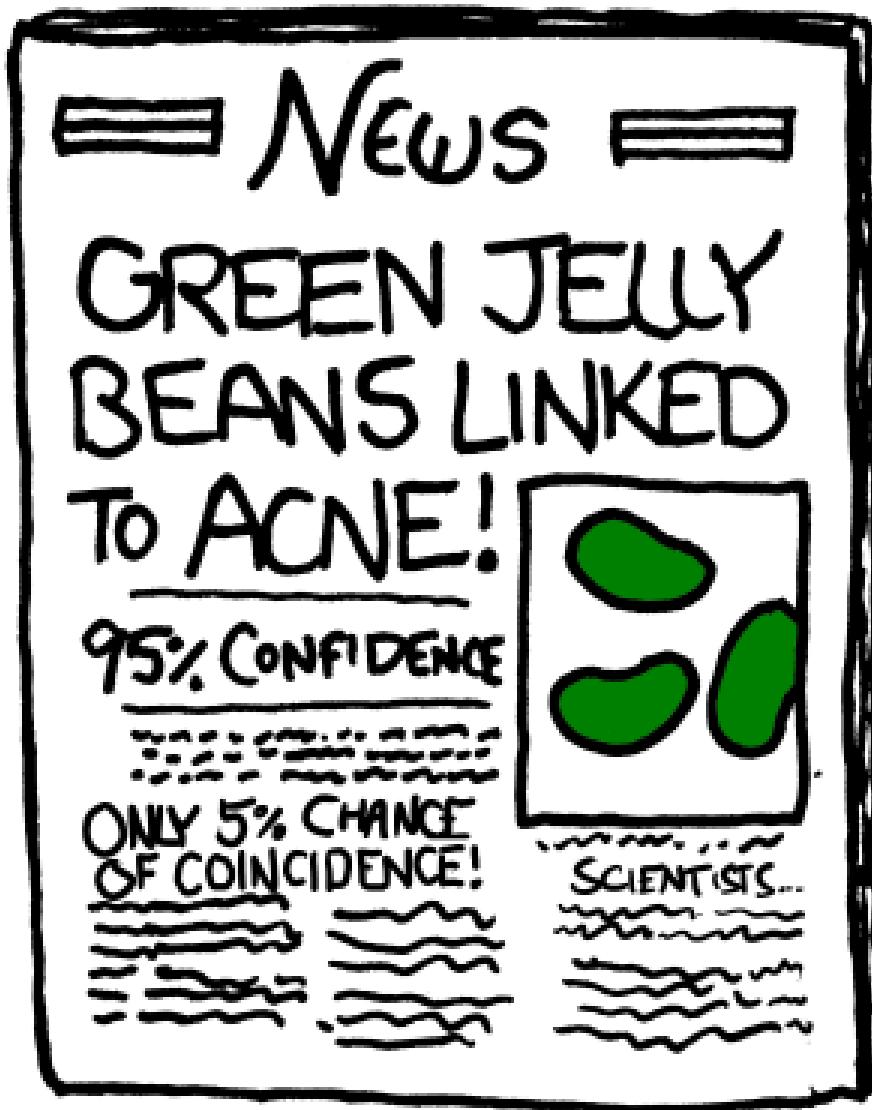
		Population Condition	
		H_0 True	H_a True
Conclusion	Accept H_0	Correct Conclusion	Type II Error
	Reject H_0	Type I Error	Correct Conclusion

False Negative, β error

False Positive, α error

Probability of an error in a multiple test:

$$1 - (0.95)^{\text{number of comparisons}}$$



<http://www.xkcd.com/882/>

edu.sablab.net/abs2016

L6.1. Multiple Comparisons

False Discovery Rate

False discovery rate (FDR)

FDR control is a statistical method used in multiple hypothesis testing to correct for multiple comparisons. In a list of rejected hypotheses, FDR controls the expected proportion of incorrectly rejected null hypotheses (type I errors).

		Population Condition		Total
		H ₀ is TRUE	H ₀ is FALSE	
Conclusion	Accept H ₀ (non-significant)	U	T	$m - R$
	Reject H ₀ (significant)	V	S	R
	Total	m_0	$m - m_0$	m

$$FDR = E\left(\frac{V}{V + S}\right)$$

False Discovery Rate

Assume we need to perform $m = 100$ comparisons,
and select maximum **FDR = $\alpha = 0.05$**

Independent tests

The **Simes procedure** ensures that its expected value $E\left[\frac{V}{V + S}\right]$ is less than a given α (Benjamini and Hochberg 1995). This procedure is valid when the m tests are **independent**. Let $H_1 \dots H_m$ be the null hypotheses and $P_1 \dots P_m$ their corresponding **p-values**. Order these values in increasing order and denote them by $P_{(1)} \dots P_{(m)}$. For a given α , find the largest k such that $P_{(k)} \leq \frac{k}{m}\alpha$.

Then reject (i.e. declare positive) all $H_{(i)}$ for $i = 1, \dots, k$.

Note that the mean α for these m tests is $\frac{\alpha(m+1)}{2m}$ which could be used as a rough FDR, or RFDR, " α adjusted for m indep. tests." The RFDR calculation shown here provides a useful approximation and is not part of the Benjamini and Hochberg method; see AFDR below.

L6.1. Multiple Comparisons

False Discovery Rate: Benjamini & Hochberg

Assume we need to perform $m = 100$ comparisons,
and select maximum **FDR = $\alpha = 0.05$**

$$FDR = E\left(\frac{V}{V + S}\right)$$

Expected value for FDR $< \alpha$ if

$$P_{(k)} \leq \frac{k}{m} \alpha$$

`p.adjust(pv, method="fdr")`

$$\frac{m P_{(k)}}{k} \leq \alpha$$

Other Methods

Bonferroni – simple, but too stringent, not recommended

Holm – a more powerful and less stringent version of Bonferroni (ok)

L6.1. Multiple Comparisons

p-value or FDR?

Let's generate a completely random experiment (script L6.1)

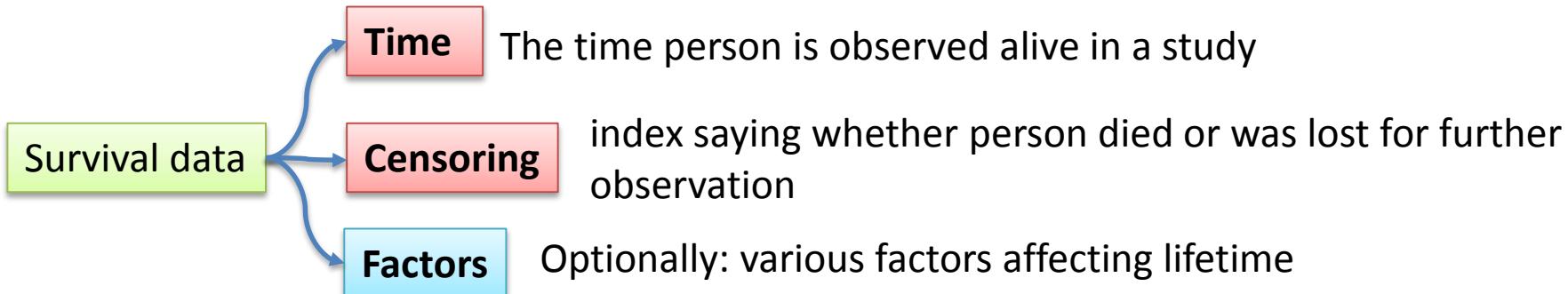
Survival Data

Survival analysis

is a branch of statistics which deals with analysis of time to events, such as death in biological organisms and failure in mechanical systems (i.e. **reliability theory** in engineering).

Survival analysis attempts to answer questions such as:

- What is the proportion of a population which will survive past a certain time?
- Of those that survive, at what rate will they die or fail?
- Can multiple causes of death or failure be taken into account?
- How do particular circumstances or characteristics increase or decrease the probability of survival?

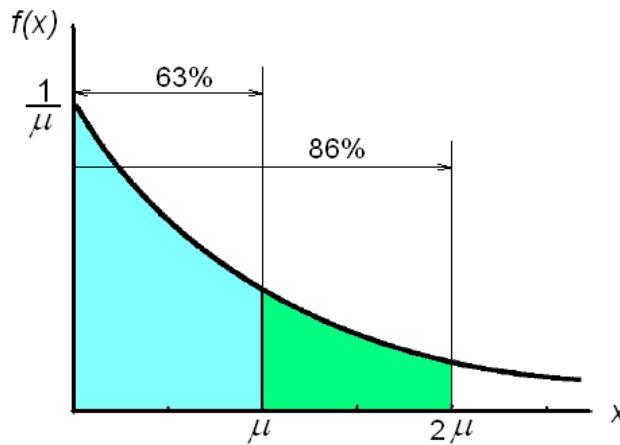


<http://www.partek.com/webinars/survival-analysis-partek-genomics-suite-software>

L6.2. Survival Analysis

Cox's Survival Model

$$f(x) = \frac{1}{\mu} e^{-\frac{x}{\mu}} \quad \text{for } x \geq 0, \mu > 0$$



$$h(t) = h_0(t) e^{\beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n}$$

$h(t)$ – hazard function

$h_0(t)$ – basic hazard

$x_1 \dots x_n$ – covariates (age, smoking, expression of gene X)
which are time-independent!

$\beta_1 \dots \beta_n$ – unknown parameters

$$HR = \frac{h_i(t)}{h_j(t)} = \exp\left\{\beta_1(x_{i1} - x_{j1}) + \dots + \beta_n(x_{in} - x_{jn})\right\}$$

To identify significantly involved covariate: partial likelihood is calculated

L6.2. Survival Analysis

```
library(survival)
str(lung)
```

```
## create a survival object
## lung$status: 1-censored, 2-dead
sData = Surv(lung$time, event = lung$status == 2)
print(sData)
```

```
## Let's visualize it
fit = survfit(sData~1)
plot(fit)
```

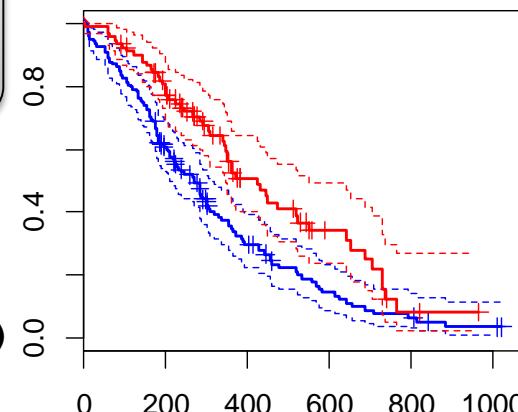
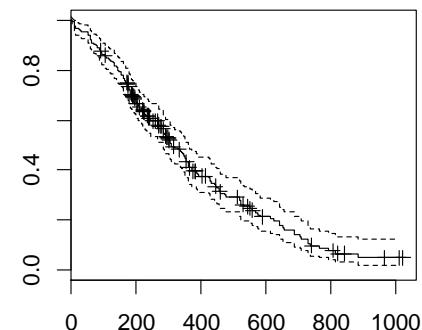
```
## Let's visualize it for male/female
fit.sex = survfit(sData ~ lung$sex)
plot(fit.sex, col=c("blue","red"), conf.int = TRUE)
```

```
## Rank test for survival data
dif.sex = survdiff(sData ~ lung$sex)
dif.sex
```

```
## build Cox regression model
mod = coxph(sData ~ sex + age, data=lung)
summary(mod)
```

Example: Lung

“event” should be:
 0 – for censored
 1 – for dead patients



ovarian

L6.3. Microarrays

Public Repositories

GEO: <http://www.ncbi.nlm.nih.gov/gds>

The screenshot shows the GEO DataSets search interface. The search term 'NCI00001350' has been entered. The results page displays 1 to 20 of 1350 entries. One entry is highlighted: 'Nodules diabetic NCI00001350 1 week old female'. The interface includes filters for 'DataSets', 'Series', 'Samples', 'Platforms', 'Organisms', 'Study type', 'Expression profiling by array', 'Wires', 'Author', 'Title', 'Attribute name', 'Tissue', 'Cell type', 'Type', 'Publication date', 'Strain', 'Custom range', 'Cross ref', and 'Show additional filters'. On the right, there's a 'Browse Content' section with links to 'Top Organisms', 'Most used platforms', 'Biosamples', 'Diseases/conditions', and 'More...'. Below this are sections for 'Find related data', 'Database', and 'Search'.

Browse Content

Repository Browser

DataSets: 3847

Series: 50810

Platforms: 13387

Samples: 1237318

TCGA: <https://tcga-data.nci.nih.gov/tcga/>

The screenshot shows the TCGA Data Portal Overview page. It features a header with the TCGA logo and 'Understanding genomics to improve cancer care'. Below the header are links for 'Home', 'Download Data', 'Tools', 'About the Data', and 'Publication Guidelines'. A sidebar on the left contains 'Announcements' with a message about TCGA DCC downtime from August 16th to 17th. The main content area is titled 'TCGA Data Portal Overview' and contains a summary of the portal's purpose: 'The Cancer Genome Atlas (TCGA) Data Portal provides a platform for researchers to search, download, and analyze data sets generated by TCGA. It contains clinical information, genomic characterization data, and high level sequence analysis of the tumor genome.' It also notes that the portal does not host lower levels of sequence data (e.g., NCI's Cancer Genomics Hub (CGHub)). A 'Download Data' button is available, along with a link to 'Choose from four ways to download data'. Below this is a table titled 'Available Cancer Types' showing the number of cases shipped by BCR and cases with data for various cancer types. At the bottom, there are links for 'More TCGA Information' and 'More information about The Cancer Genome Atlas'.

ArrayExpress: <http://www.ebi.ac.uk/arrayexpress/>

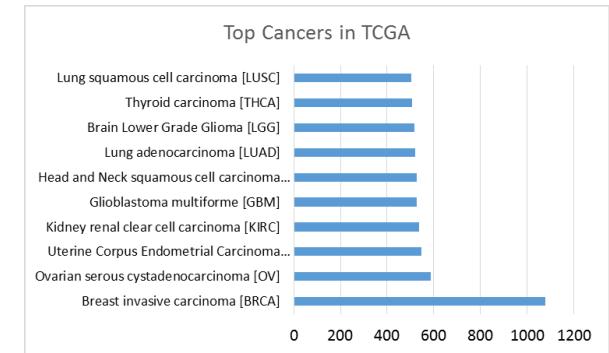
The screenshot shows the ArrayExpress experiments search interface. The search term 'E-MEXP-3544' has been entered. The results page displays 1 to 10 of 10 experiments. One experiment is highlighted: 'E-MEXP-3544 - Transcription profiling by array of human malignant melanoma cell line, A375, following interferon-gamma-induced gene transcription'. The interface includes filters for 'Status', 'Organism', 'Samples (10)', 'Array (1)', and 'Protocols (6)'. Below the search results, there is a detailed description of the experiment, mentioning microRNAs as major regulators of post-transcriptional gene regulation and STAT1 as a key regulator. The description also discusses the dynamic behavior of miRNAs over time and co-ordinated dynamic transcription of several clustered miRNAs.

Data Content

Updated today at 06:00

- 52801 experiments
- 1555904 assays
- 24.99 TB of archived data

Sep 2014 – more than 10k patients



Analysis via:
<http://www.cbioportal.org/public-portal/>

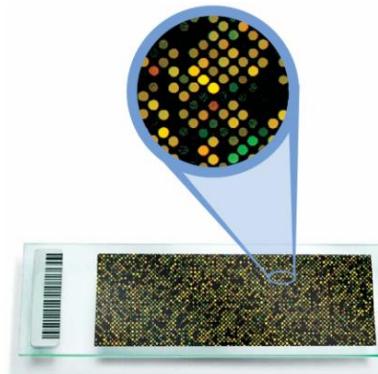
Data for our course: <http://edu.sabl.net/transcript>

L.6.3. Microarray Data

Types of Microarrays

Two-color Arrays (2C)

- ◆ Agilent full genome
- ◆ Thematic arrays



Pro

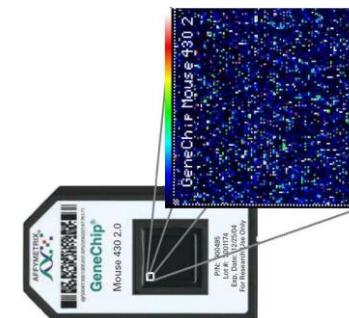
- ◆ Direct comparison
- ◆ Less sensitive to inaccuracies of spotting

Con

- ◆ Dye effects: need for “dye-swaps”
- ◆ Non-flexibility in analysis

One-color Arrays (1C)

- ◆ Affymetrix GeneChip
- ◆ Affymetrix Exon
- ◆ Affymetrix mRNA



Pro

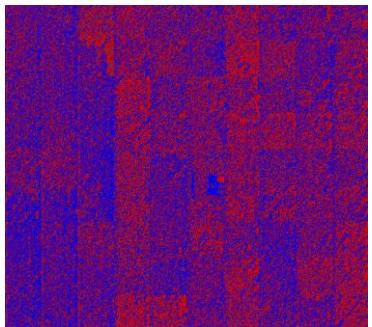
- ◆ Flexible analysis
- ◆ High level of standardization

Con

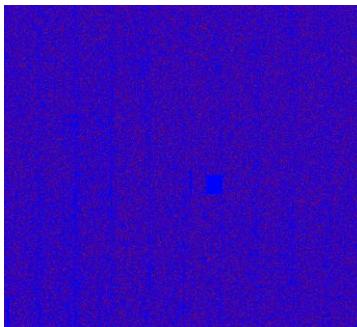
- ◆ Price

One-color Arrays

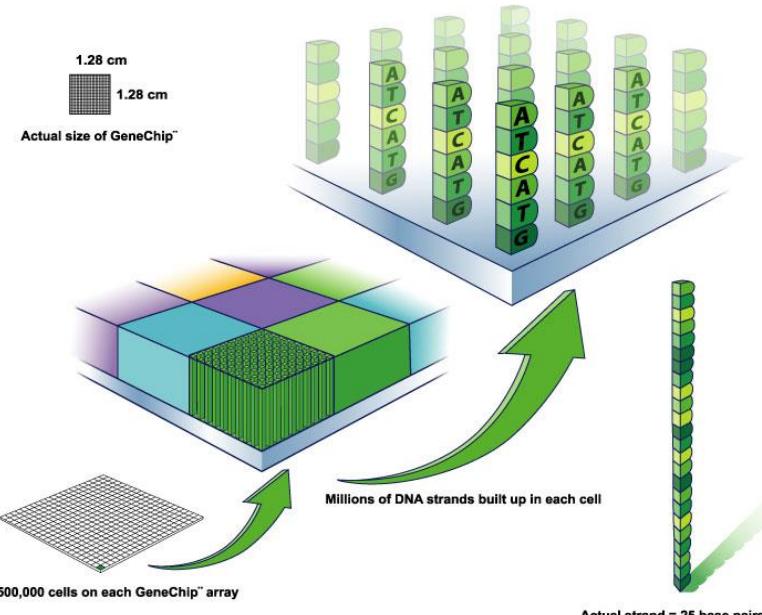
Raw



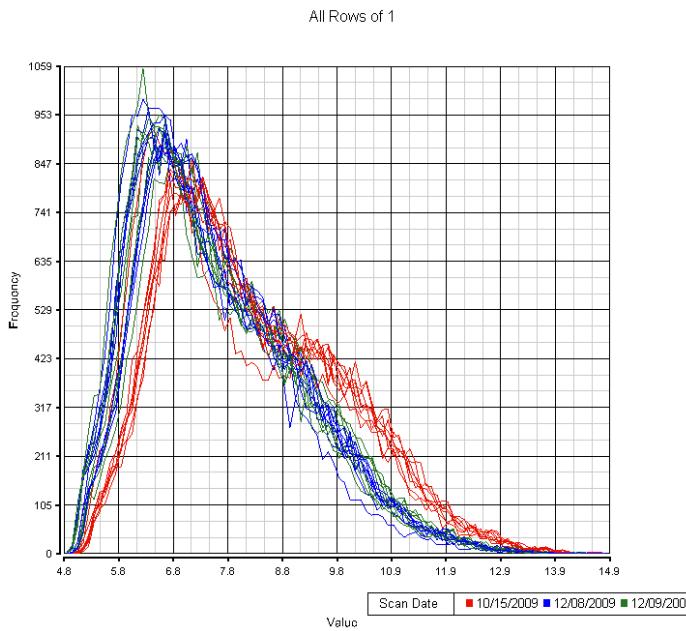
Normalized



High reproducibility and quality of spotting is required.
Affymetrix – “photolithography”-like technique



$$\text{LogIntensity} = \log_2(I)$$



Background is “removed” during normalization step

Filtering may help removing uninformative features

Affymetrix: Probes, Probesets and Transcript clusters

Probes

25-mer sequences targeted on a single region of transcriptome (hopefully)

Probesets

groups of closely located or overlapped probes (on average 4 probes)

Exons

HuExon and HTA arrays allow measuring exon expression

Transcript clusters

For majority of features - synonymous to "genes". However, some distinct transcripts of genes are considered as different transcript clusters.

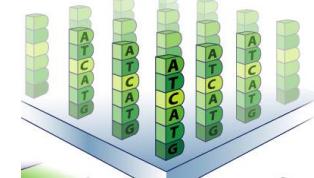
In old versions of Affy arrays (hgu95, hgu133, etc), there were:

PM – perfect match probes

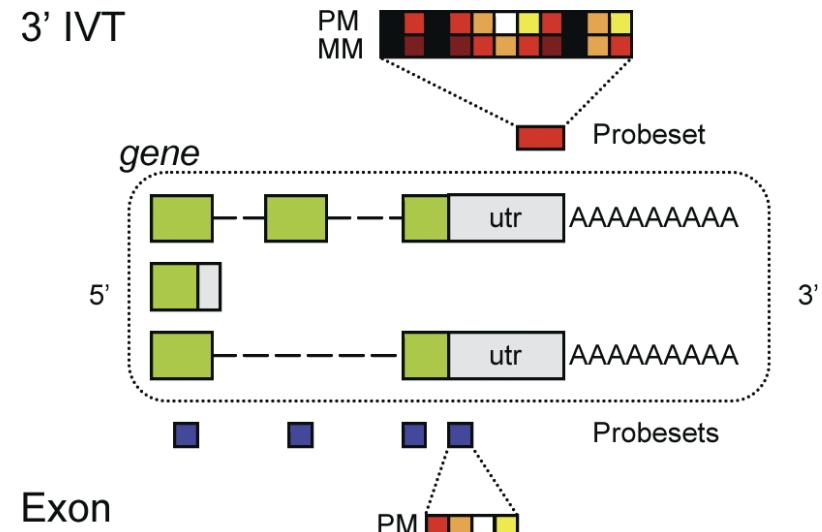
MM – mismatch probes (having replacement in th 13th character)

This was done for background estimation.

But this approach is not used now!!



3' IVT



Okoniewski M, Comprehensive Analysis of Affymetrix Exon Arrays Using BioConductor, PLoS CompBiol, 2008

Normalization of Affymetrix Arrays by RMA

Background
correction



Normalization
b/w arrays



Estimate
expression

Background and signal are strictly positive.
Noise is additive in log scale:

$$PM_{ij} = \underset{\text{exponential}}{S_{ijn}} + \underset{\text{normal}}{B_{ijn}}$$

Quantile **normalization** b/w arrays: makes distribution of probes the same across all arrays

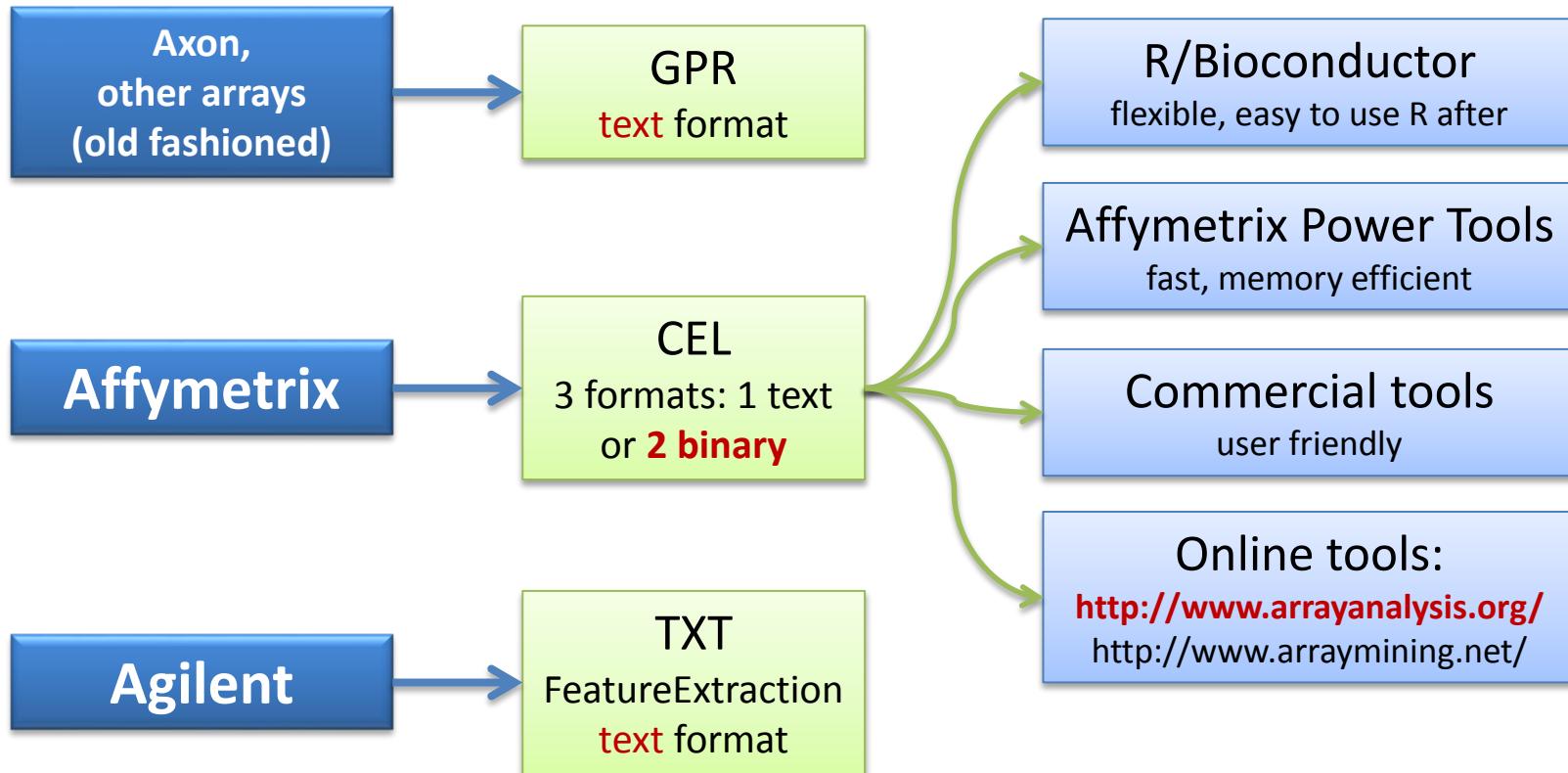
Probeset expression is estimated from a linear model:

$$Y_{ijn} = \underset{\text{observed}}{\mu_{in}} + \underset{\text{probe affinity}}{\alpha_{jn}} + \underset{\text{error with 0 mean}}{\varepsilon_{ijn}}$$

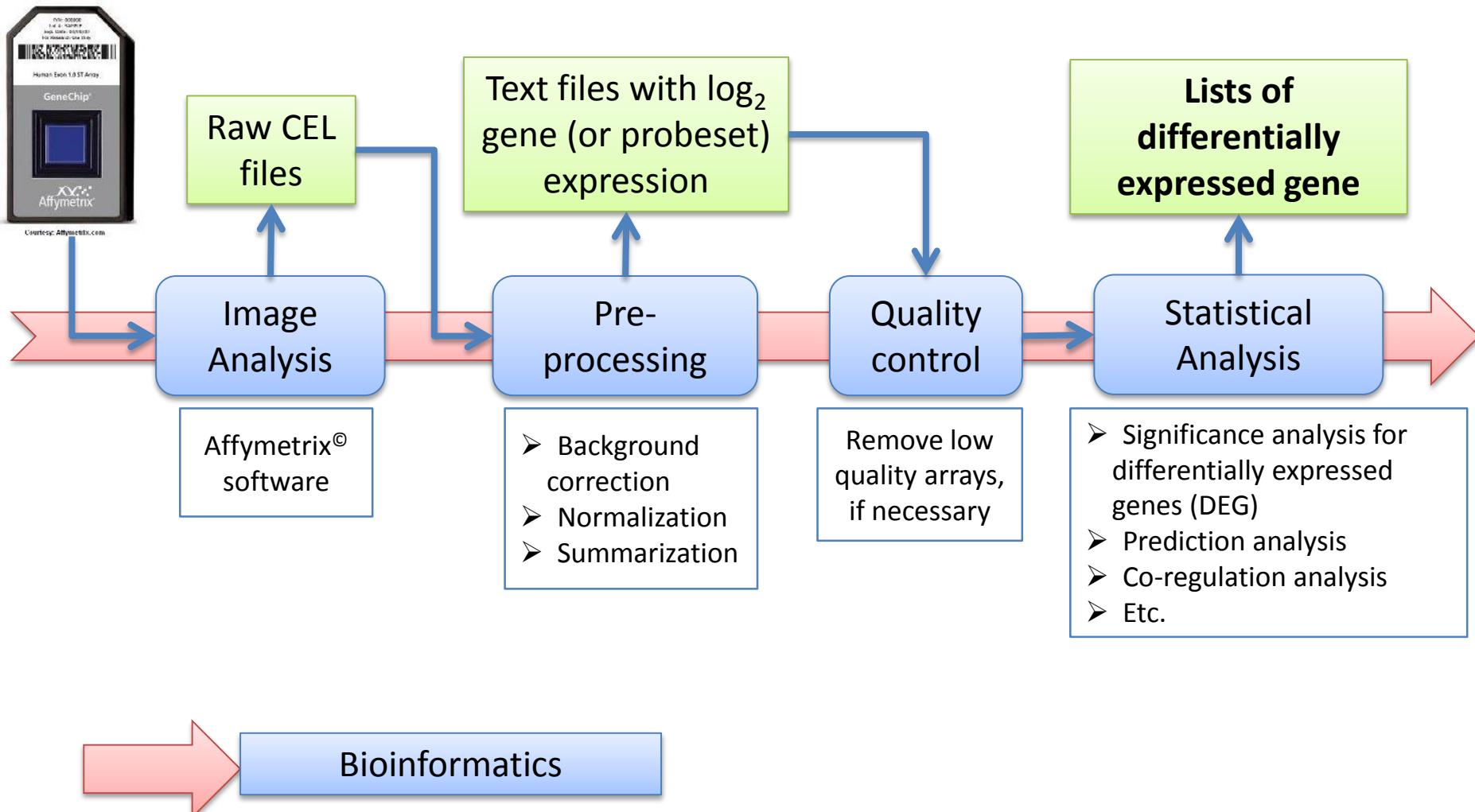
i – array
j – probe
n – probeset

“Median polish” helps avoid outliers effect

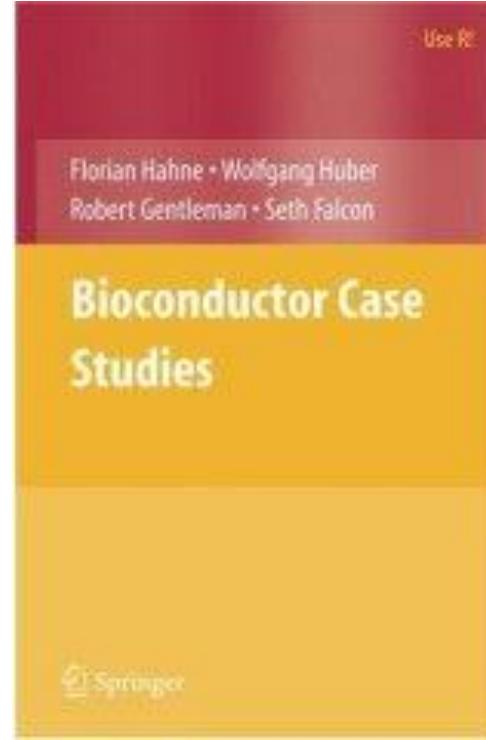
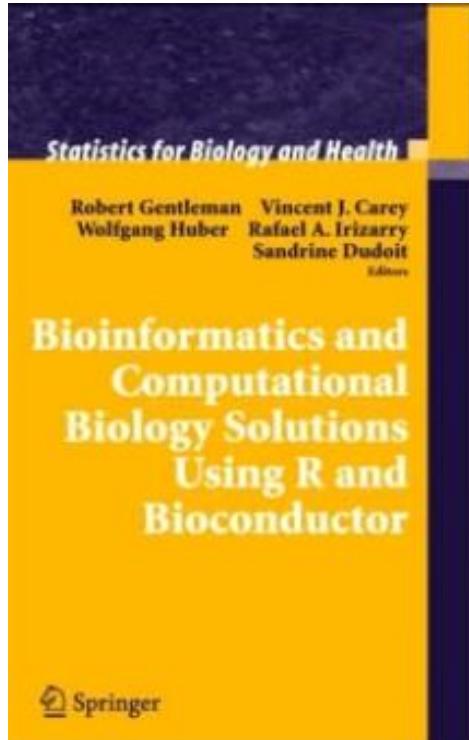
File Formats



Analysis Pipeline



R / Bioconductor



Affymetrix Power Tools

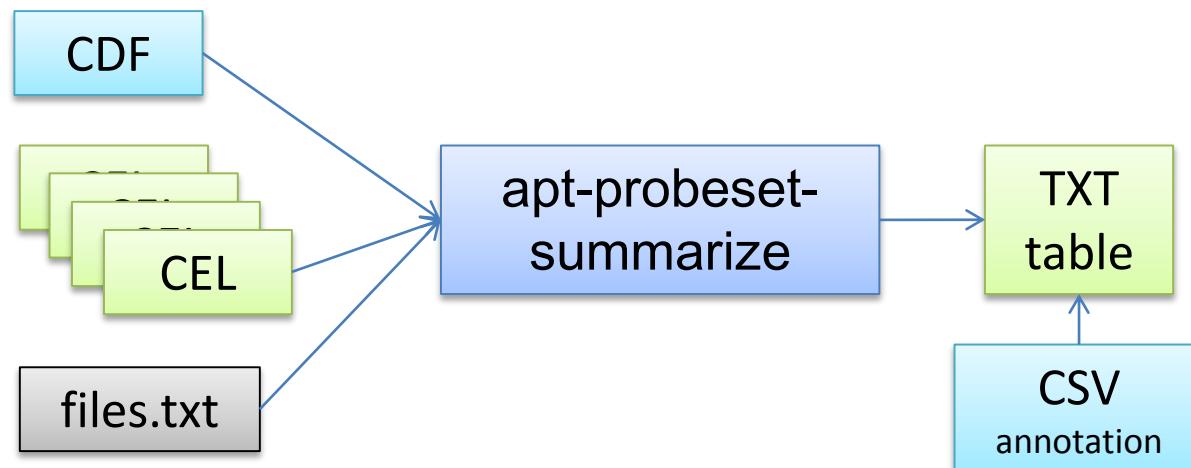
apt-probeset-summarize is a program for doing background subtraction, normalization and summarizing probe sets from Affymetrix expression microarrays. It implements analysis algorithms such as [RMA](#), [PLIER](#), and DABG (detected above background).

The main features of **apt-probeset-summarize** not common in other implementations are: Quantile normalization using a subset (sketch) of the data which results in much smaller memory usage.

<http://www.affymetrix.com/support/developer/powertools/changelog/apt-probeset-summarize.html>

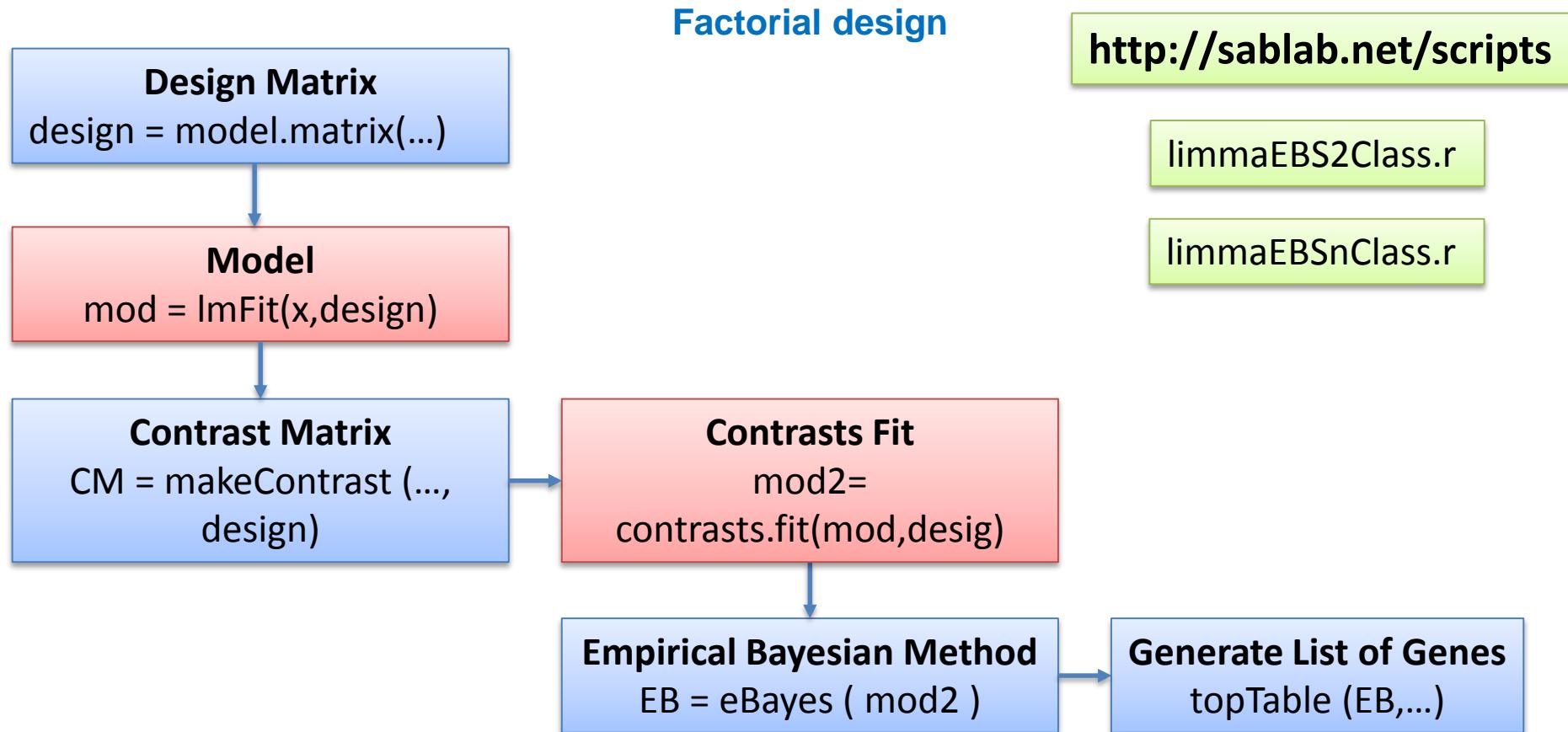
apt-probeset-summarize

```
-a rma-sketch -d chip.cdf -o output-dir --cel-files files.txt
```



<http://edu.sablab.net/data/gz/>

Differential Expression Analysis



Differential Expression Analysis

<http://edu.sablab.net/data/txt/lusc.zip>

1. Find genes significantly differentially expressed in SCC vs normal tissue

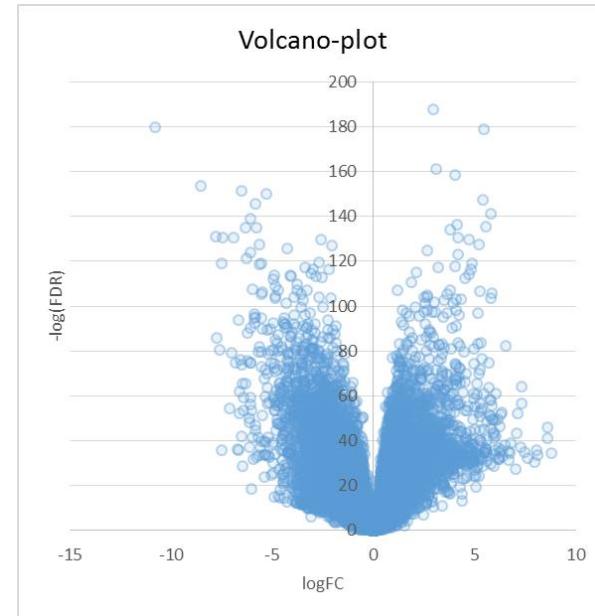
- apply *limma*
- Keep genes with FDR > 0.001
- keep only genes with $|\log FC| > 2$

2. Make a “volcano plot”:

- $\log_{10}(FDR)$ vs LogFC

3. Save lists of up and down regulate genes –
we shall need them

<http://sablab.net/scripts>



L6.3. Microarray Data Analysis

```
#####
# L6.2. Import and Analysis
#####
## clear memory
rm(list = ls())
#####
## L6.2.1. Loading results after APT and QC
#####
## load data after APT
## alternative: http://edu.sablab.net/data/gz/rma-sketch.summary.txt
Data = read.table("e:/data/kreis/+data+/miR.pub/cel/res/rma-sketch.summary.txt",
                  header=T, sep="\t", as.is=T)

## load sample description
## alternative: http://edu.sablab.net/data/gz/Affymetrix_miRNA2.txt
Meta= read.table("e:/data/kreis/+data+/miR.pub/cel/files.txt",
                  header=T, sep="\t", as.is=T)
str(Data)
Meta

## keep only human miRNA
Data = Data[grep("hsa-",Data$probeset_id),]

# if order of Data columns and Meta rows are the same - simply change columns
if (sum(names(Data)[-1])!= Meta[,1]) == 0) names(Data)[-1] = Meta[,2]

source("http://sablab.net/scripts/plotDataPDF.r")
x11()
plotDataPDF(Data,add.legend=T,col=rainbow(ncol(Data)))
x11()
boxplot(Data[,-1],outline=F,col=rainbow(ncol(Data)),las=2)

#####
## L6.2.2 Analysis
#####
## let's filter out miR with low expression
## and put the rest into matrix Y
thr = 3
idx.keep = logical(nrow(Data))|T
idx.keep[apply(Data[,-1],1,max)<=thr]=F
sum(idx.keep)

## Y contains now the data
Y = as.matrix(Data[idx.keep,-1])
colnames(Y) = names(Data)[-1]
rownames(Y) = sub("_st","",Data[idx.keep,1])
str(Y)

## plot heatmap of scaled data
heatmap(t(scale(t(Y)))) 

## plot PCA
PC = prcomp(t(Y))
## plot 3D
library(rgl)
plot3d(PC$x[,1],PC$x[,2],PC$x[,3],
       size = 2,
       col = rainbow(ncol(Data)),
       type = "s",
       xlab = "PC1",
       ylab = "PC2",
       zlab = "PC3")
text3d(PC$x[,1]+0.5,PC$x[,2]+0.5,PC$x[,3]+0.5,colnames(Y))

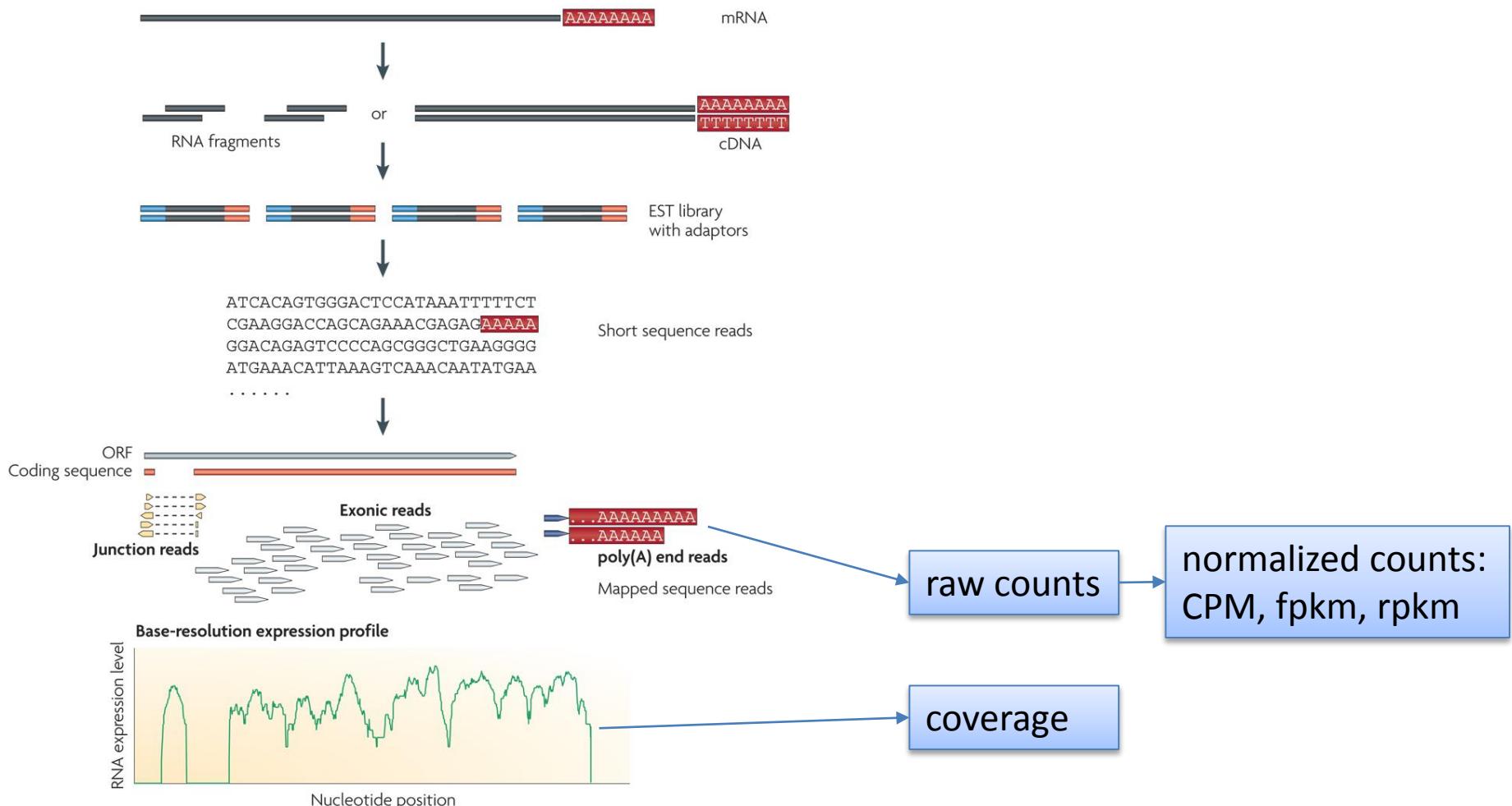
## DEA
source("http://sablab.net/scripts/limmmaEBS2Class.r")

idx=c(grep("T000",colnames(Y)),
      grep("T48",colnames(Y)))
res=limmmaEBS2Class(Y[,idx],rownames(Y),classes=c("T00","T00","T48","T48"),
                     plotTop=20)
```

RNASeq

6.4. RNA-Seq Data

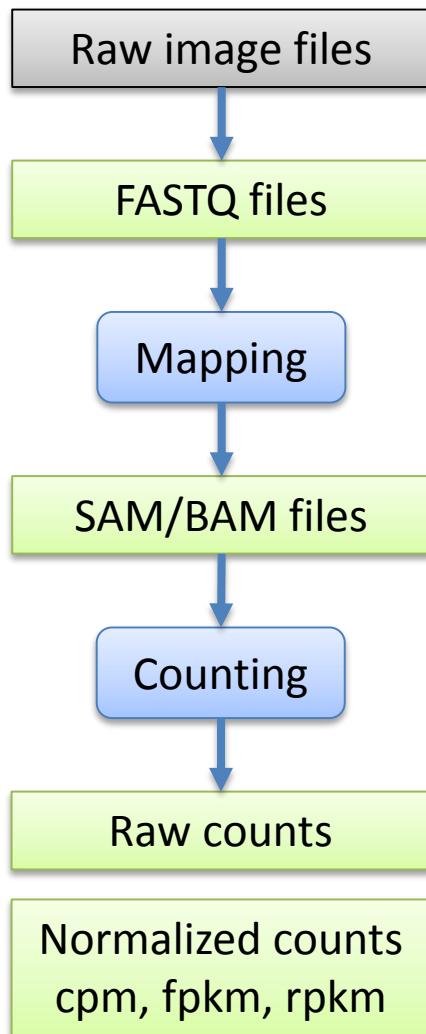
Next Generation Sequencing: RNA-Seq



Wang Z et al. RNA-Seq: a revolutionary tool for transcriptomics. *Nat Rev Genet.* 2009

6.4. RNA-Seq Data

File Types



```
@HWI-ST508:152:D06G9ACXX:2:1101:1160:2042 1:Y:0:ATCACG  
NAAGACCGAATTCTCCAAGCTATGGTAAACATTGCACTGGCCTTCATCTG  
+  
#11??+2<<<CCB4AC?32@+1@AB1**1?AB<4=4>=BB<9=>?#####
```

Read – a short sequence identified in RNA-Seq experiment
Library – set ($10^5 - 10^8$) of reads from a single sample

```
@HD      VN:1.0 SO:coordinate  
@SQ      SN:seq1 LN:5000  
@SQ      SN:seq2 LN:5000  
@CO      Example of SAM/BAM file format.
```

```
B7_591:4:96:693:509 73 seq1      1          99          36M      *  
          0          0          CACTAGTGGCTCATTGTAAATGTGTGGTTAACTCG  
          <<<<<<<<<<<<<<< ;<<<<<<< 5 <<<<< ; : < ; 7  
          MF:i:18     Aq:i:73     NM:i:0      UQ:i:0      H0:i:1  
  
H1:i:0EAS54_65:7:152:368:113    73          seq1      3          99  
          35M      *          0          0          CTAGTGGCTCATGTAAATGTGTGGTTAACTCGT  
          <<<<<<< 0 <<<< 655 << 7 <<< 9 << 3 / << 6 : MF:i:18      Aq:i:66  
          NM:i:0      UQ:i:0      H0:i:1      H1:i:0
```

For the list of tools see:

http://en.wikipedia.org/wiki/List_of_RNA-Seq_bioinformatics_tools

6.4. RNA-Seq Data

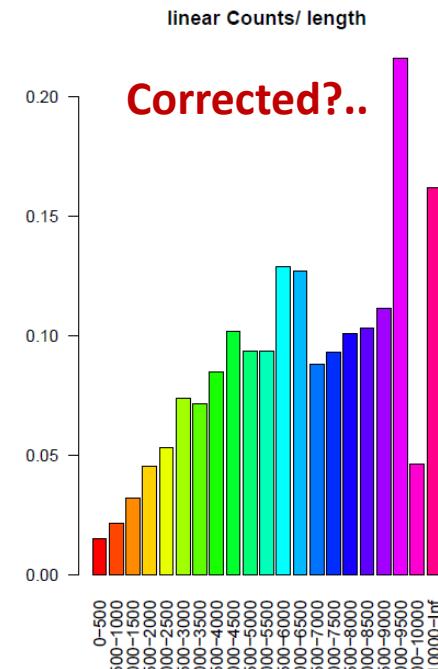
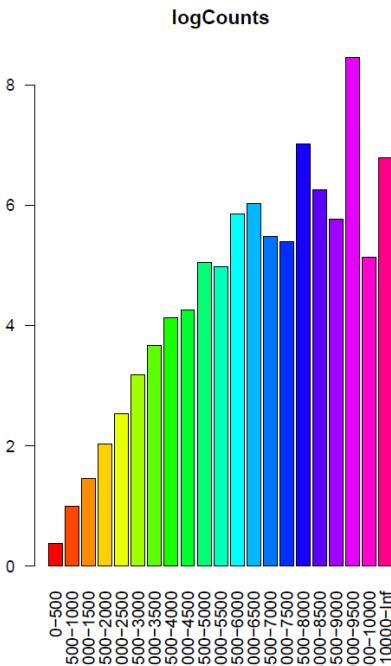
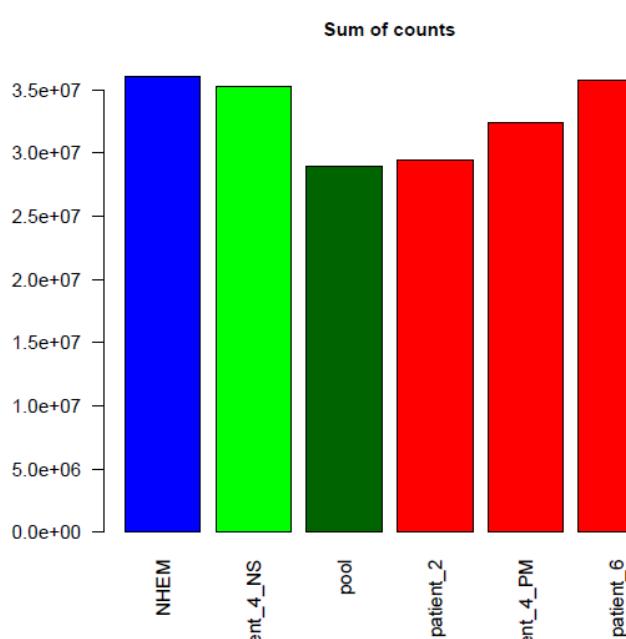
Normalization

Problems:

- ◆ Libraries has different size (different number of reads from samples)
- ◆ Long transcripts produce more reads

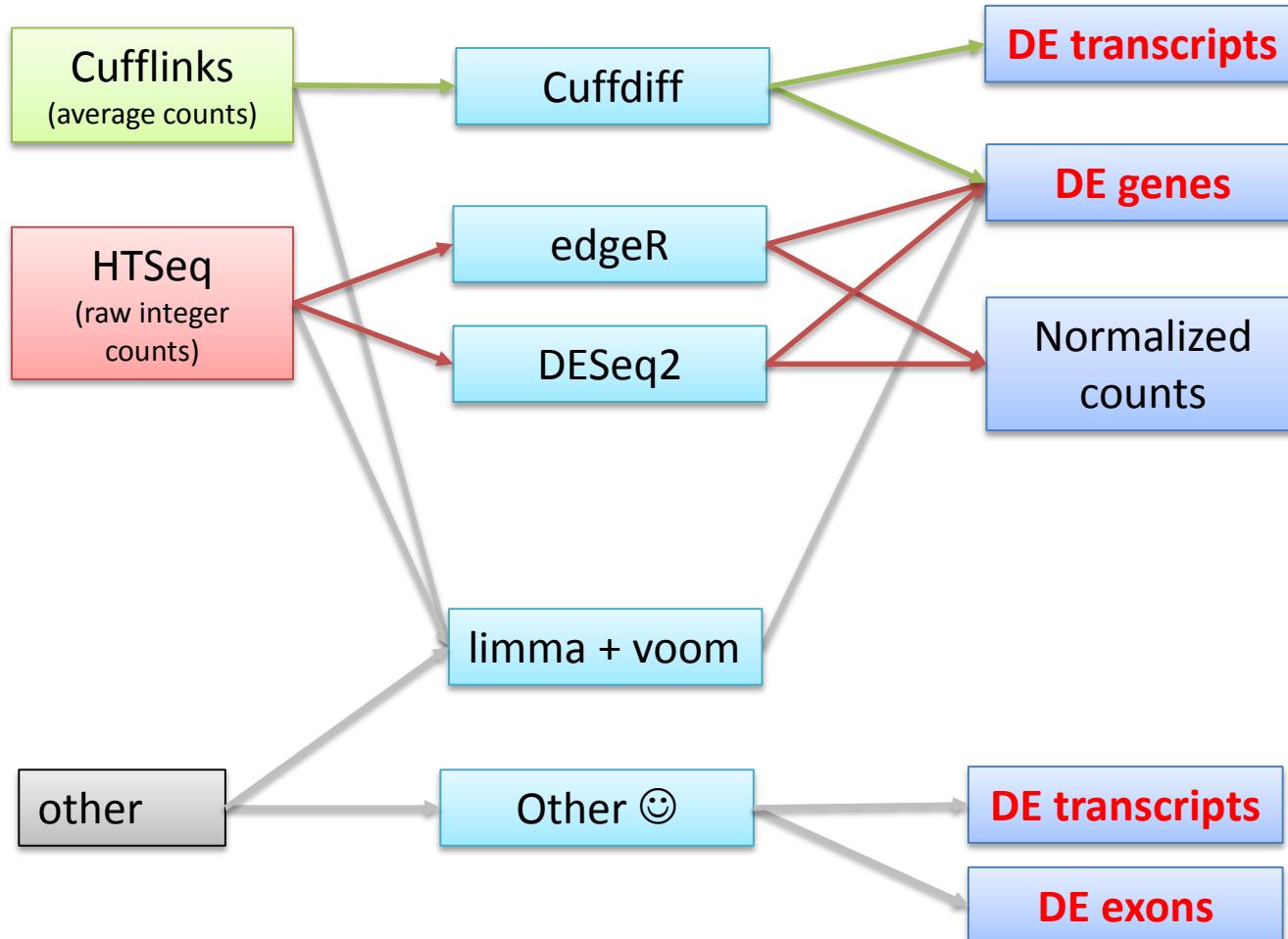
Solutions (?) :

- ◆ Accounting for library size during analysis (standard) or direct correction for it
- ◆ Correction for transcript size (but which transcript is expressed?)



6.4. RNA-Seq Data

Differential Expression Analysis



Differential Expression Analysis (edgeR)

<https://sablab.net/scripts>

LibDEA.r

Differential Expression Analysis (DESeq2)

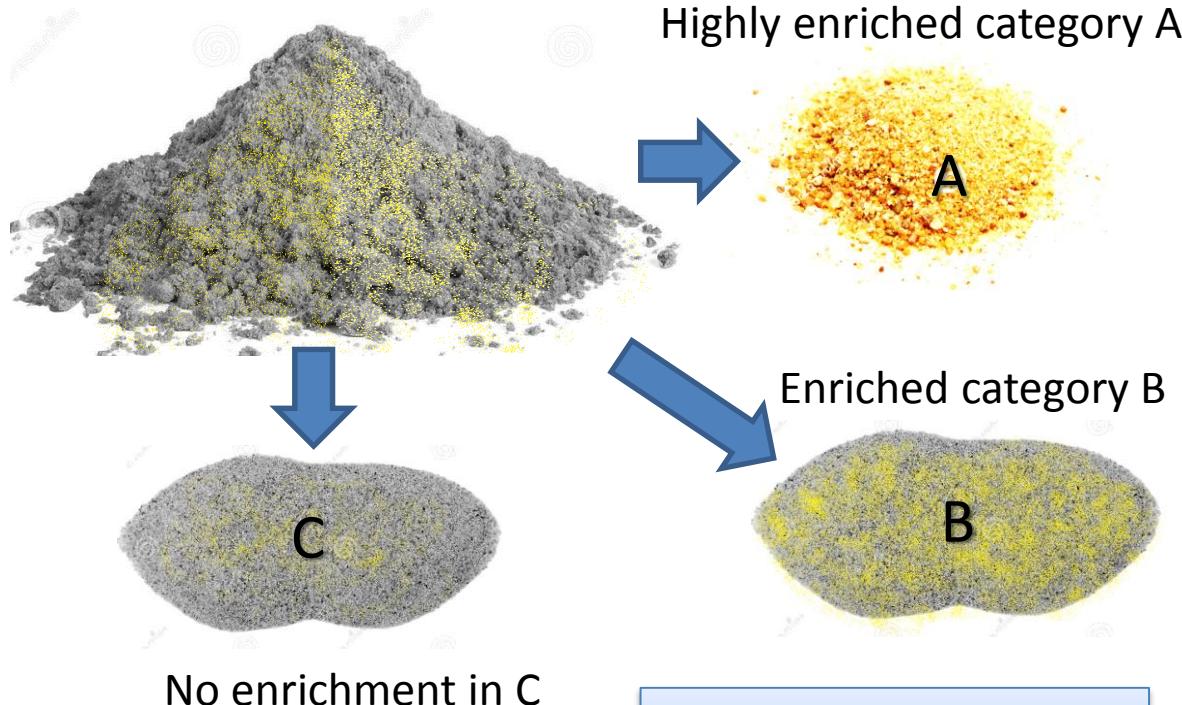
<https://sablab.net/scripts>

LibDEA.r

Enrichment Analysis

1. Category Enrichment Analysis

Are interesting genes overrepresented in a subset corresponding to some biological process?



Method of the analysis:
Fisher's exact test

Someone grabs “randomly”
20 balls from a box with
100x ● and 100x ●

How surprised will you be if
he grabbed
●●●●●●●●●●●●●●●●●●●●●●●●
(17 red , 3 green)

sand belongs to: [http://www.dreamstime.com/photos-images/pile-sand.html ;\)\)](http://www.dreamstime.com/photos-images/pile-sand.html ;)))

1. Category Enrichment Analysis

Fisher's exact test: based on hypergeometrical distributions

Hypergeometrical: distribution of objects taken from a “box”, without putting them back

$$P = 1 - \sum_{i=0}^{k-1} \frac{\binom{M}{i} \binom{N-M}{n-i}}{\binom{N}{n}}$$

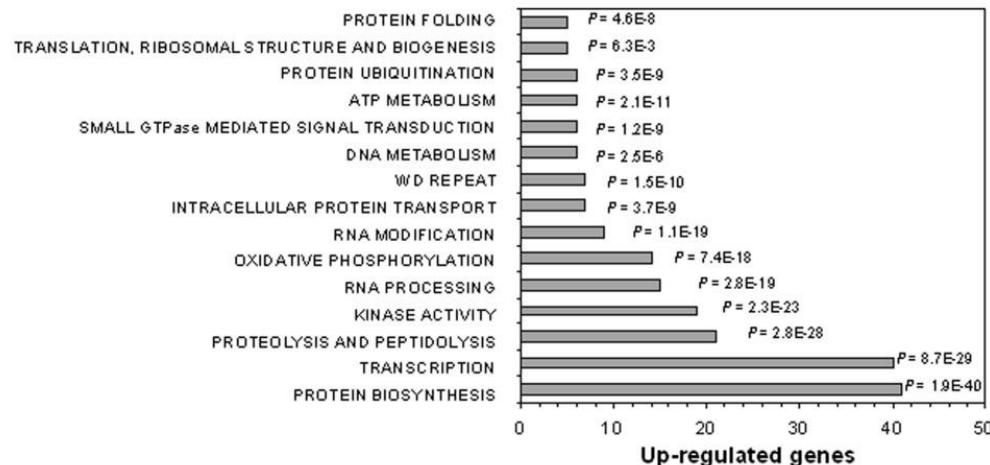
N: total number of genes

M: total number of genes annotated with this term

n: number of genes in the list

k: number of genes in the list annotated with this term

$$C_k^n = C_n^k = \binom{n}{k} = \frac{n!}{k!(n-k)!}$$

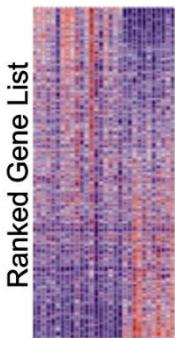


Okamoto et al. Cancer Cell International 2007 7:11 doi:10.1186/1475-2867-7-11

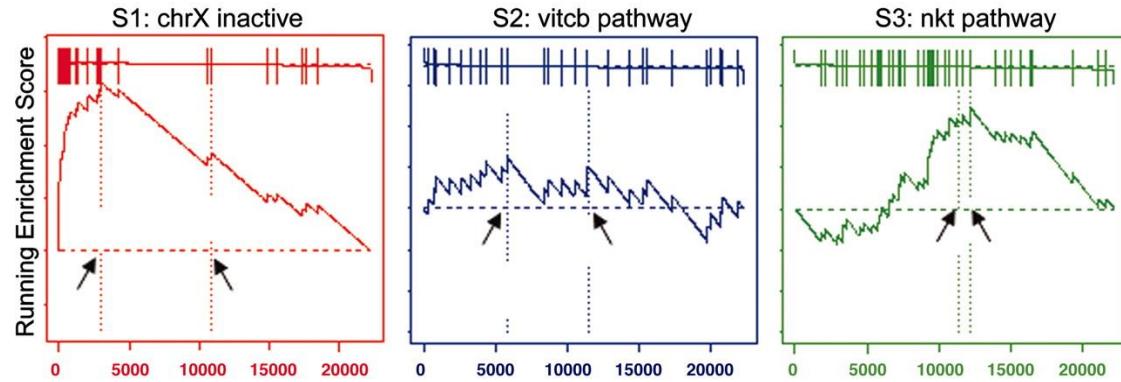
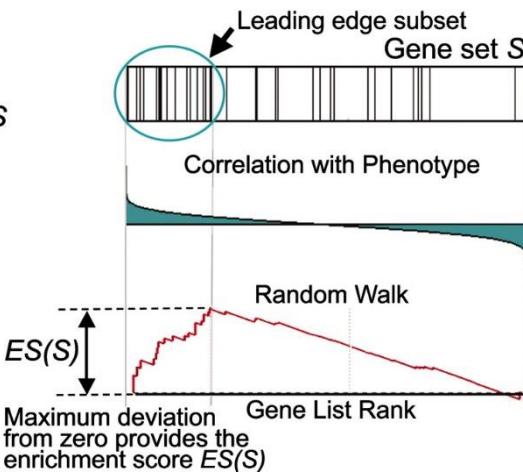
2. Gene Set Enrichment Analysis (GSEA)

Is direction of genes in a category random?

A Phenotype Classes
A B



B
Gene set S



A. Subramanian et al. PNAS 2005, 102, 43

Example: GO enrichment

<http://edu.sablab.net/transcript>

Strategy 1:

Take all DEG and use them in enrichment.

- Safe
- No additional assumptions
- Cannot distinguish \uparrow and \downarrow functions

Strategy 2:

Separate DEG to down- and up- regulated genes. Then perform independent enrichment by these 2 groups

- Can be biased (gene can be $\uparrow\downarrow$)
- Assume \uparrow gene $\Rightarrow \uparrow$ function
- Can distinguish \uparrow and \downarrow functions

Enrichr

<http://amp.pharm.mssm.edu/Enrichr/enrich>

BioCompendium

<http://biocompendium.embl.de/>

L6.5. Enrichment Analysis

LUSC Example

<http://edu.sablab.net/data/txt/lusc.zip>

0. Prepare lists of DE genes...

1. Put up-regulated into **enrich**

3. Check: Down CMAP, Disease Signatures from GEO up,

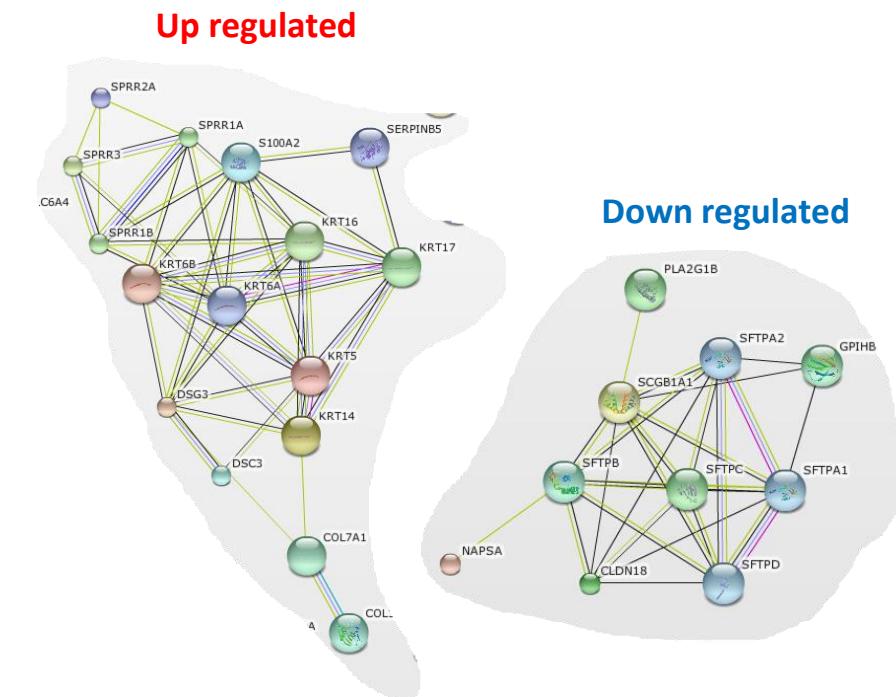
4. Try **biocompendium**

5. Put top 100 genes into String to see PP-interactions

<http://amp.pharm.mssm.edu/Enrichr/>

<http://biocompendium.embl.de/>

<http://string-db.org>



In R

```
#####
## enrichGOens - warup for topGO package: enrichment analysis of GO-terms
## based on Ensembl IDs
##
## genes - vector with list of ENSEMBL IDs (character)
## fdr - vector of FDR for each gene (numeric)
## fc - vector of logFC for each gene (numeric)
## thr.fdr - significance threshold for FDR (numeric)
## thr.fc - significance threshold for absolute logFC (numeric)
## db - name of GO database: "BP","MF","CC" (character)
## genome - R-package for genome annotation used. For human - 'org.Hs.eg.db' (character)
## do.sort - if TRUE - resulted functions sorted by p-value (logical)
## randomFraction - for testing only, the fraction of the genes to be randomized (numeric)
##
## (c)GNU GPL P.Nazarov 2014. petr.nazarov[at]crp-sante.lu
#####
```

<https://sablab.net/scripts>

enrichGOens.r

```
enrichGOens =
function(genes,fdr,fc,thr.fdr=0.05,thr.fc=0,db="BP",genome="org.Hs.eg.db",do.sort=TRUE,
randomFraction=0){
  ## load libraries
  if (!require(genome,character.only=TRUE)){
    cat("MESSAGE enrichGO: ",genome," package is not found. Installing...\n",sep="")
    source("http://bioconductor.org/biocLite.R")
    biocLite(genome)
    library(genome,character.only=TRUE)
  }
  if (!require("topGO")){
    cat("MESSAGE enrichGO: ' topGO ' package is not found. Installing...\n")
    source("http://bioconductor.org/biocLite.R")
    biocLite("topGO")
    library("topGO")
  }
  if (!exists("sortDataFrame")) source("http://sablab.net/scripts/sortDataFrame.r")
  ## prepare gene categories and score
  myGO2genes <- annFUN.org(db, mapping = "org.Hs.eg.db", ID = "ensembl")
  score = (-log10(fdr)*abs(fc))
  names(score)=genes
  score[fdr>=thr.fdr | abs(fc)<=thr.fc]=0

  ## add randomness if required, to test stability
  if (randomFraction>0){
    ## define remove probability: low score have more chances
    prob1 = 1/(1+score)
    prob1[is.na(prob1)]=0
    prob1[score == 0] = 0
    ## define add probability: high score has more chances
    prob2 = -log10(fdr)*abs(fc)
    prob2[is.na(prob2)]=0
    prob2[score > 0] = 0
    ## add and remove
    n=round(sum(score>0)*randomFraction)
    score[sample(1:length(genes),n,n,prob=prob2)]=1+rexp(n,1/mean(score[score>0]))
    score[sample(1:length(genes),n,n,prob=prob1)]=0
  }
  ## create topGOdata object
  SelectScore = function(sc){return(sc>0)} ## simple function for significance
  GOdata = new("topGOdata", ##constructor
              ontology = db,
              allGenes = score,
              geneSelectionFun = SelectScore,
              annot = annFUN.GO2genes,
              GO2genes = myGO2genes)
  ## run testing
  resFisher = runTest(GOdata, algorithm = "classic", statistic = "fisher")
  ## transform results into a table
  enrichRes = GenTable(GOdata, classicFisher = resFisher,
                       ranksOf = "classicFisher",topNodes = length(resFisher@score))
  enrichRes$classicFisher[grep("<",enrichRes$classicFisher)] = "1e-31"
  enrichRes$classicFisher = as.double(enrichRes$classicFisher)
  enrichRes$FDR = p.adjust(enrichRes$classicFisher,"fdr")
  enrichRes$Score = -log10(enrichRes$FDR)
  ## by default sorted by p-value. If needed - sort by ID
  if (!do.sort) enrichRes = sortDataFrame(enrichRes,"GO.ID") ## remove sorting
  return(enrichRes)
}
```

Thank you for your attention !

